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Heat and mass transport behavior in bio-convective reactive flow of nanomaterials with Soret and Dufour characteristics

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ABSTRACT

The main of this article is to analyze magnetohydrodynamic bioconvective flow of Sutterby nanoliquid. Gyrotactic microorganism in presence of chemical reaction is addressed. Thermophoretic, magnetic field, random motion heat generation and radiation are discussed. Furthermore, Dufour and Soret behaviors are taken into account. Thermal conduction augmentation performance is discussed by utilization Boungiorno's model. Nonlinear PDE's (partial differential equations) are changed to ordinary system through appropriate variables. To developed computational solutions, we used the ND-solve technique. Results for temperature, microorganism field, liquid flow, and concentration are exhibited through different emerging variables. The physical quantities like Nusselt number, microorganism density number and solutal transport rate for various sundry variables are presented. Summary of main results re highlighted in the conclusions. Velocity reduces against magnetic field, while reverse trend seen for buoyancy ratio variable. Thermal distribution has an enhancing trend for magnetic and radiation variables. An enhancement in concentration distribution is seen for Soret number.

1. Introduction

Bioconvection is due to the up swimming of microorganisms caused due to density gradient and becomes unstable or destabilized. In the fluidic environment microorganisms display extensive versatility in swimming directions. The happening of bioconvection gives a modern way of mixing and controlling mass transport in diverse fluid flow problems. Bioconvection is a new kind of convection which is essential in biologic polymerization mixtures, ecosystem, oil recovery system and hydrogen fuel. Aziz et al. [1] studied the bioconvection flow of hybrid nanoliquid within presence of motile microorganism due to stretched porous medium. Solutal and thermal transfer analysis for bioconvective slip flow of nanoliquid towards stretching/shrinking medium is explained by Uddin et al.

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Fig. 1. Flow diagram.

[2]. Thermal transport analysis in bioconvective flow of nanoliquid considering motile microorganism is illustrated by Kuznetsov [3]. Bioconvection stratified magnetohydrodynamic flow of Oldroyd-B nanoliquid with microorganism field considering heat source due stretched wall is executed by Waqas et al. [4]. Performance of activation energy in bioconvection magnetized Williamson material in presence of radiation influence is examined by Asjad et al. [5]. Alsaedi et al. [6] reported the heat and solutal transfer rate analysis in bioconvection MHD flow of nanoliquid containing motile microorganisms. Zhang et al. [7] elaborated the hydromagnetic bioconvective flow of Williamson nanoliquid containing microorganism saturated in Darcy-Forchheimer medium. Recently, various researchers and investigators works on multiple innovative concept regarding interlayer exchange coupling [8], entropy optimized reactive flow with Ohmic heating [9], bio-inspired magnetism-responsive hybrid micro-structures [10], velocity slip flow with ternay nanofluid [11], first hidden charm penta-quark [12], bio-convective Maxwell fluid flow [13] and modeling of nano-graphite film and vapor-liquid equilibrium for electrolyte solutions [14,15].

Recently, nanofluids have been proven to be very effective as base fluid due to their remarkable thermophysical properties (density, thermal conductivity, viscosity and specific heat) in heat transfer rate. Nanofluids are fluids which contain nanometer sized particle. The nanoparticles are very small size same as to de Brogile or coherent wavelength. Because of this nanoparticles action like energy materials. Nanofluids are the homogeneous mixture of nanometer sized particles (1-100 nm) in a conventional fluid. Recent engineers and scientists have received much attention about nanoliquid due to essential thermal properties. An improvement of the thermal efficiency of their exchangers is one of the various application of this material. Nanoliquids having applications likes vehicle cooling, nanowires, nanofibers, cancer therapy, engine cooling, fuel cells, inorganic lungs, domestic refrigerator, pharmaceutical processes, electronic cooling system and radiators etc. Choi and Eastman [16 and 17] were the first who introduced the concept of nanofluids. Choi investigated thermal conductivity of nanomaterials. Afterwards many researchers explored the mechanisms of nanofluid in different geometrical domains. Due to a wide variety of applications in science and technology nanofluids have attained much attention by researchers and scientists. Nanofluids are primarily used in heat transfer equipment, in solar collectors, polymerase chain reaction and many others. After that Buongiorno [18] gave the theoretical model and described the seven-slip characteristics for heat transportation in nanoliquid. Reddy and Makinde [19] investigated buoyancy forces, thermophoretic and random movement for hydrodynamic Jeffrey nanoliquid flow. Irreversibility and radiation analysis for chemically reactive MHD nanoliquid flow is investigated by Khan et al. [20]. Variable viscosity impact in propylene glycol-based hybrid nanoliquid flow with heat generation is illuminated by Khan et al. [21]. Wang et al. [22], Zhang et al. [23] and Xiang et al. [24] highlight thermal evolution of chemical structure, advanced energy materials and directional fluid spreading on micro-fluidic chip structure respectively. Rasool et al. [25,26] numerically explored MHD Al2O3-Cu/engine oil based flow and EMHD non-Darcian flow towards a Riga surface. Khan et al. [27] and Li et al. [28,29] examined reactive based fluid flow with different flow geometries. Further discussions in this direction are given as follows: numerical solution for multi-layer granular bed filter [30], radiative flow for four different types of nanoparticles with non-uniform heat source [31], micropolar nanofluid flow through lid driven cavity [32], fluid flow analysis in the presence of chemical reaction [33,34], non-Darcian nano fluid flow and bio-convective processes for cross nanofluid [35,37] and Arrhenius activation energy impact in fluid flow [36,38].

Objective of recent analysis is to explore the bioconvective hydromagnetic Sutterby nanoliquid flow. Motile microorganism along with thermophoretic and random movement are addressed. Heat generation, magnetohydrodynamic effect and radiation are scrutinized in energy expression. Additionally, Soret and Dufour characteristics are taken into consideration. ND-solve technique is utilized to get numerical solutions for the given dimensionless expression. Outcomes of secondary variables on temperature, microorganism field, velocity and concentration are analyzed. Physical analysis of heat transfer rate, microorganism density number and solutal transfer rate versus flow variables are examined.

2. Formulation

Consider three-dimensional bioconvective magnetized flow of Sutterby nanomaterial. Buongiorno's model along with motile microorganism is addressed. Thermal radiation, magnetohydrodynamic effect and heat generation are taken into consideration. Furthermore, Soret and Dufour behaviors are taken into account. Magnetic field of strength (B_0) is applied. Surface is stretched bidirectional having velocities $u_w(=ax)$, $v_w(=by)$ with a, b > 0. Fig. 1 presents flow diagram.

The related expressions are given by [39-42]:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0,$$
(1)

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} + w\frac{\partial u}{\partial z} = \nu_f \frac{\partial^2 u}{\partial z^2} \left[1 - \frac{\beta^2}{6} \left(\frac{\partial u}{\partial z} \right)^2 \right]^n - \frac{n\nu_f \beta^2}{3} \left(\frac{\partial u}{\partial z} \right)^2 \times \frac{\partial^2 u}{\partial z^2} \left[1 - \frac{\beta^2}{6} \left(\frac{\partial u}{\partial z} \right)^2 \right]^{n-1}$$

$$\frac{\sigma_f B_0^2}{\rho_f} u + \frac{1}{\rho_f} \left(\rho_f (1 - C_\infty) (T - T_\infty) g\beta^* - \left(\rho_p - \rho_f \right) (C - C_\infty) g - \left(\rho_m - \rho_f \right) (N - N_\infty) g\gamma^* \right) \right\},$$
(2)

$$u\frac{\partial v}{\partial x} + v\frac{\partial v}{\partial y} + w\frac{\partial v}{\partial z} = \nu_f \frac{\partial^2 v}{\partial z^2} \left[1 - \frac{\beta^2}{6} \left(\frac{\partial v}{\partial z} \right)^2 \right]^n - \frac{n\nu_f \beta^2}{3} \left(\frac{\partial v}{\partial z} \right)^2 \frac{\partial^2 v}{\partial z^2} \times \left[1 - \frac{\beta^2}{6} \left(\frac{\partial v}{\partial z} \right)^2 \right]^{n-1} - \frac{\sigma_f B_0^2}{\rho_f} v = 0 \right\},$$
(3)

$$u\frac{\partial T}{\partial x} + v\frac{\partial T}{\partial y} + w\frac{\partial T}{\partial z^2} = \alpha_f \frac{\partial^2 T}{\partial z^2} + \tau \left(D_B \frac{\partial C}{\partial z} \frac{\partial T}{\partial z} + \frac{D_T}{T_\infty} \left(\frac{\partial T}{\partial z} \right)^2 \right) + \frac{\sigma_f B_0^2}{\rho_f} \left(u^2 + v^2 \right) + \frac{16\sigma^* T_\infty^3}{3k^* \left(\rho c_p\right)_f} \frac{\partial^2 T}{\partial z^2} + \frac{D_B k_T}{c_p C_s} \frac{\partial^2 C}{\partial z^2} + \frac{Q_0}{\left(\rho c_p\right)_f} \left(T - T_\infty \right) \bigg\},$$
(4)

$$u\frac{\partial C}{\partial x} + v\frac{\partial C}{\partial y} + w\frac{\partial C}{\partial z} = D_B\frac{\partial^2 C}{\partial z^2} + \frac{D_T}{T_\infty}\frac{\partial^2 T}{\partial z^2} + \frac{D_Bk_T}{T_m}\frac{\partial^2 T}{\partial z^2} - k_r^2(C - C_\infty),$$
(5)

$$u\frac{\partial N}{\partial x} + v\frac{\partial N}{\partial y} + w\frac{\partial N}{\partial z} + \left(\frac{\partial}{\partial z}\left(N\frac{\partial C}{\partial z}\right)\right)\frac{b^*W_c}{(C_w - C_\infty)} = D_m\frac{\partial}{\partial z}\left(\frac{\partial N}{\partial z}\right)$$
(6)

With [39-42]:

$$u = U_w = ax, v = V_w = by, w = 0, -k_f \frac{\partial T}{\partial z} = h_f(T_w - T), -D_B \frac{\partial C}{\partial z} = h_m(C_w - C), -D_m \frac{\partial N}{\partial z} = h_k(N_w - N) \quad \text{at } z = 0$$

$$u \to 0, v \to 0, T \to T_\infty, C \to C_\infty \ N \to N_\infty \quad \text{as } z \to \infty$$

$$\left. \right\}$$

$$(7)$$

Here (u, v, w) denotes the velocity components, n power law index, (x, y, z) Cartesian coordinates, β material constant, k_T thermal diffusion ratio, Q_0 heat source coefficient, b^* chemo taxis constant, $(\rho c_p)_p$ effective heat capacity of nanoparticles, h_m mass transfer rate, β^* volume expansion coefficient, D_T thermophoresis coefficient, W_c cell swimming speed, T_w wall temperature, C_∞ ambient concentration, N_w wall microorganism concentration, C concentration, σ_f electrical conductivity, γ^* microorganism average volume, h_f heat transfer rate, β_0 magnetic field strength, h_k microorganism transfer rate, C_s concentration susceptibility, ρ_f density, α_f thermal diffusivity, g gravity, T temperature, N_∞ ambient microorganism concentration, k_f thermal conductivity, c_p specific heat, k_r reaction rate, T_∞ ambient temperature, T_m mean fluid temperature, σ^* Stefan-Boltzman constant, D_m swimming microorganism coefficient, ρ_m microorganism density, ρ_p nanoparticle density, $(\rho c_p)_f$ heat capacity of fluid, ν_f kinematic viscosity, C_w wall concentration, D_B

Brownian motion coefficient, *N* microorganism concentration, k^* mean absorption coefficient and $\tau \left(= \frac{(\rho c_p)_p}{(\rho c_p)_f} \right)$ ratio of capacities. Considering [43]:

$$u = axf'(\eta), v = ayg'(\eta), w = -\sqrt{ax}(f(\eta) + g(\eta)), \theta(\eta) = \frac{T - T_{\infty}}{T_w - T_{\infty}} \left\{ \varphi(\eta) = \frac{C - C_{\infty}}{C_w - C_{\infty}}, \chi(\eta) = \frac{N - N_{\infty}}{N_w - N_{\infty}}, \eta = z\sqrt{\frac{a}{\nu_f}} \right\}.$$
(8)

We have

Table 1

Nusselt number results comparison with Lone et al. [44].

Pr	Lone et al. [44]	Recent outcomes
0.72	0.463144	0.4631135
1.0	0.581976	0.5819757
3.0	1.165245	1.1652449
7.0	1.895403	1.8954046
10.0	2.308003	2.3080025



Fig. 2. $f'(\eta)$ via M.



Fig. 3. $g'(\eta)$ via M.



(9)



Fig. 4. $f'(\eta)$ via λ .



Fig. 5. $f'(\eta)$ via N_r .



Fig. 6. $f'(\eta)$ via α_2 .



Fig. 7. $\theta(\eta)$ via Du.



Fig. 8. $\theta(\eta)$ via M.



Fig. 9. $\theta(\eta)$ via Nb.

$$\left(1 - \frac{\alpha_2}{6}g'^2\right)^n g''' - \frac{n\alpha_2}{3} \left(1 - \frac{\alpha_2}{6}g''^2\right)^{n-1} g''^2 g''' + (f+g) g'' - g'^2 - Mg' = 0 \bigg\},$$
(10)

$$(1+Rd) \theta'' + \Pr(f+g) \theta' - \Pr f \theta' + \Pr Du \varphi'' + M \Pr Ec(f'^2 + g'^2) \\ \Pr(Nb\theta' \varphi' + Nt\theta'^2 + Q\theta) = 0$$

$$(11)$$

$$\varphi'' + Le(f+g) \varphi' - f\varphi' + \frac{Nt}{Nb}\theta'' - \gamma Le\varphi + LeSr\theta'' = 0,$$
(12)

$$\chi'' + Lb(f+g)\chi' - Pe(\Omega\varphi'' + \chi\varphi'' + \varphi\chi') = 0,$$
(13)

with





$$\begin{cases} f'(0) = 1, f(0) = 0, g'(0) = \in, g(0) = 0 \ \theta'(0) = -\beta_1(1 - \theta(0)), \\ \varphi'(0) = -\beta_2(1 - \varphi(0)), \chi'(0) = -\beta_3(1 - \chi(0)) \\ f'(\infty) = 0, g'(\infty) = 0, \theta(\infty) = 0, \varphi(\infty) = 0, \chi(\infty) = 0 \end{cases}$$
(14)

Here $Rd\left(=\frac{16\sigma^{*}T_{\infty}^{*}}{3k^{*}k_{f}}\right)$ indicates the radiation variable, $Le\left(=\frac{\nu_{f}}{D_{B}}\right)$ the Lewis number, $\lambda\left(=\frac{g\beta^{*}(T_{w}-T_{\infty})(1-C_{\infty})}{a\rho_{f}}\right)$ the mixed convection variable, $\epsilon\left(=\frac{b}{a}\right)$ the ratio parameter, $\alpha_{1}\left(=\frac{b^{2}a^{3}x^{2}}{\nu_{f}}\right)$ the material variable, $\beta_{2}\left(=\frac{h_{m}}{D_{B}}\sqrt{\frac{\nu_{f}}{a}}\right)$, solutal Biot number, $N_{r}\left(=\frac{(\rho_{p}-\rho_{f})(C_{w}-C_{\infty})}{\rho_{f}\beta^{*}(T_{w}-T_{\infty})(1-C_{\infty})}\right)$ the Buoyancy ratio parameter, $\beta_{1}\left(=\frac{h_{f}}{k_{f}}\sqrt{\frac{\nu_{f}}{a}}\right)$, thermal Biot number, $R_{b}\left(=\frac{(\rho_{m}-\rho_{f})(N_{w}-N_{\infty})\gamma^{*}}{\rho_{f}(T_{w}-T_{\infty})(1-C_{\infty})\beta^{*}}\right)$ the bioconvective Rayleigh number, $Lb\left(=\frac{\nu_{f}}{D_{m}}\right)$ the bioconvective Lewis number, $M\left(=\frac{\sigma_{f}B_{0}^{2}}{a\rho_{f}}\right)$ the magnetic variable, $Pe\left(=\frac{bW_{c}}{D_{m}}\right)$ the Peclet number, $Q\left(=\frac{Q_{0}}{a(\rho c_{p})_{f}}\right)$ the heat generation variable, $\Pr\left(=\frac{\nu_{f}}{a_{f}}\right)$ the Prandtl number, $\alpha_{2}\left(=\frac{\beta^{2}a^{3}\gamma^{2}}{\nu_{f}}\right)$ the material variable, $\gamma\left(=\frac{k_{r}}{a}\right)$ the reaction variable, $\beta_{3}\left(=\frac{h_{k}}{D_{m}}\sqrt{\frac{\nu_{f}}{a}}\right)$ microorganism Biot number, $Ee\left(=\frac{(ax)^{2}}{(c_{p})_{f}(T_{w}-T_{\infty})}\right)$ the Eckert number, $Nt\left(=\frac{\tau D_{T}(T_{w}-T_{\infty})}{\nu_{f}T_{\infty}}\right)$, the thermophoresis parameter, $Nb\left(=\frac{(ax)^{2}}{(c_{p})_{f}(T_{w}-T_{\infty})}\right)$



Fig. 13. $\varphi(\eta)$ via Le.

 $\frac{\tau D_B(C_w - C_w)}{\nu_f}$), the Brownian motion parameter and $\Omega\left(=\frac{N_w}{(N_w - N_w)}\right)$ the microorganism difference parameter.

3. Quantities of interest

3.1. Nusselt number

Mathematically it is

$$Nu_x = \frac{xq_w}{k_f(T_w - T_\infty)},$$
(15)

 q_w heat flux satisfies

$$q_w = -\left(k_f + \frac{16\sigma^* T_{\infty}^3}{3k^*}\right) \left(\frac{\partial T}{\partial z}\right)\Big|_{z=0},\tag{16}$$

Dimensionless equation is

$$Nu_{x} \mathbf{R} \mathbf{e}_{x}^{-1/2} = -(1+Rd) \, \dot{\theta}(0). \tag{17}$$



Fig. 14. $\varphi(\eta)$ via Nb.



Fig. 15. $\varphi(\eta)$ via Nt.

3.2. Sherwood number

It is expressed as

$$Sh_{x} = \frac{xj_{w}|_{z=0}}{D_{B}(C_{w} - C_{\infty})},$$
(18)

here j_w mass flux is defined as

$$j_w = -D_B \left(\frac{\partial C}{\partial z}\right),\tag{19}$$

We get

$$Sh_x \operatorname{Re}_x^{-1/2} = -\varphi'(0).$$

3.3. Microorganisms density number

It is given as

(20)



Fig. 16. $\chi(\eta)$ via *Lb*.



Fig. 17. $\chi(\eta)$ via *Pe*.

$$Sn_{x} = \frac{xj_{n}|_{z=0}}{D_{m}(N_{w} - N_{\infty})},$$
(21)

in which j_n microorganism flux is

$$j_n = -D_m \left(\frac{\partial N}{\partial z}\right). \tag{22}$$

One can found

$$Sn_{x}\operatorname{Re}_{x}^{-1/2} = -\chi'(0).$$
 (23)

In above equations $\operatorname{Re}_x = \frac{ax^2}{\nu_f}$ represents the local Reynolds number.

Results for thermal transport rate.

Nt	Nb	Rd	Nu _x
0.1	0.2	1.2	0.589609
0.3			0.584711
0.5			0.578188
0.7			0.56769
0.8	0.2	1.2	0.565881
	0.3		0.574718
	0.4		0.574501
	0.5		0.57325
0.1	0.2	0.3	0.332234
		0.6	0.420791
		0.9	0.506546
		1.2	0.589609

Table 3

Numerical outcomes for solutal transfer rate.

Sr	Nt	Nb	Sh _x
0.1	0.1	0.2	0.167237
0.2			0.165988
0.3			0.164744
0.4			0.163503
0.1	0.02	0.2	0.172212
	0.4		0.170944
	0.06		0.169691
	0.08		0.168455
0.1	0.3	0.1	0.169406
	0.6		0.170502
	0.6		0.171619
	1.2		0.172819

Table 4

Computational outcomes for microorganism density number.

Lb	Ре	Sn _x
0.6 0.7 0.8 0.9 0.7	0.1 0.01 0.05 0.09 0.13	0.0890018 0.0898872 0.0905972 0.0911799 0.0872824 0.0884499 0.0896017 0.0896017

4. Discussion

This section is organized for discussions of liquid flow, microorganism field, temperature, physical quantities and concentration. Comparison analysis of recent investigations with previous published analysis of Lone et al. [44] is mentioned in Table 1. Clearly one can found that both results are in an excellent agreement.

4.1. Velocity

Figs. (2 and 3) illustrates the flow $(f'(\eta), g'(\eta))$ variation for magnetic field. Higher magnetic field induces more disturbance in flow region and the velocities $(f'(\eta), g'(\eta))$ declined. Variation of (λ) on velocity is disclosed in Fig. 4. Clearly the fluid flow $(f'(\eta))$ is noticed an increasing function of mixed convection variable. Fig. 5 elucidates the behavior of $(f'(\eta))$ against buoyancy ratio variable. An increment in velocity is seen for larger estimation of buoyancy ratio variable. Fig. 6 sketched to show velocity $(g'(\eta))$ impact (α_2) . Higher approximation of (α_2) corresponds to upsurges the velocity field.

4.2. Temperature

Feature of Dufour number on $(\theta(\eta))$ is exhibited in Fig. 7. An increase in thermal distribution is detected via higher estimation of Dufour (*Du*) number. Fig. 8 depicts ($\theta(\eta)$) against (*M*). With higher (*M*) the resistive forces induce more resistance the flow system. As a result, the temperature upsurges. Figs. (9 and 10) are displayed to examine thermal ($\theta(\eta)$) distribution for random (*Nb*) and thermophoresis (*Nt*) variables. Clearly one can detected that thermal ($\theta(\eta)$) field upsurges for both random (*Nb*) and thermophoresis (*Nt*)

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diffusion variables. Fig. 11 depicts the magnification in ($\theta(\eta)$) with increasing (*Rd*). Clearly higher radiation (*Rd*) results into creation of more heat inside system which cause increase in temperature.

4.3. Concentration

The action of $(\varphi(\eta))$ through (*Sr*) is depicted in Fig. 12. As anticipated the Concentration $(\varphi(\eta))$ distribution is boosted via larger Soret (*Sr*) number. Fig. 13 indicates $(\varphi(\eta))$ variation via (*Le*). Physically Lewis number has inverse relation with mass diffusivity. So far big Lewis number the liquid has small mass diffusivity, as a consequence $(\varphi(\eta))$ decreases. Concentration field behavior subject to random (*Nb*) and thermophoresis (*Nt*) variables are disposed in Figs. (14 and 15). An increase in concentration has been detected for higher values of (*Nt*), while reverse impact occurs for (*Nb*).

4.4. Microorganism field

Trend of $(\chi(\eta))$ for higher bioconvection Lewis number is shown in Fig. 16. The microorganism $(\chi(\eta))$ field is decayed for larger values of (*Lb*). The action of $(\chi(\eta))$ through Peclet (*Pe*) number is shown in Fig. 17. Clearly a reduction occurs in microorganism $(\chi(\eta))$ field for larger values of Peclet (*Pe*) number.

4.5. Engineering quantities

Here heat transfer rate (Nu_x) microorganism density number (Sn_x) and solutal transport rate (Sh_x) are discussed.

4.5.1. Thermal transport rate

Variation of influential variables (like Nt, Nb and Rd) on (Nu_x) is mentioned in Table 2. A reduction in heat transport (Nu_x) rate is witnessed for higher (Nt) and (Nb). The Nusselt (Nu_x) number is boosted with increasing radiation variable.

4.5.2. Mass transport rate

Impact of Soret (*Sr*) number, random (*Nb*) and thermophoretic (*Nt*) variable is highlighted in Table 3. Obviously (*Sh_x*) is improved versus random (*Nb*) variable. Solutal transport (*Sh_x*) rate decrement is detected for higher (*Nt*) and (*Nb*).

4.5.3. Microorganisms density number

Microorganism density (Sn_x) number variation against (Lb) and (Pe) is mentioned in Table 4. There is an increase in (Sn_x) occurs for Peclet number. Microorganism density number (Sn_x) enhancement is noticed for bioconvection Lewis number.

5. Closing remarks

The following main results are mentioned:

Decreasing impact for velocities ($f'(\eta), g'(\eta)$) occurs through magnetic field.

- Increase in flow is detected for buoyancy ratio variable.
- The velocity is boosted against mixed convection variable.
- Increase in temperature is noticed for Dufour (Du) number and magnetic (M) field.
- Thermal distribution improves via larger values of thermophoresis (Nt) and random (Nb) motion variables.
- Radiation effect leads to upsurges thermal distribution and Nusselt number.
- Decreasing in heat transport rate is detected for increasing values of (Nt) and (Nb).
- Lewis number leads to reduce concentration.
- Concentration for (Nt) and (Nb) has reverse impacts.
- An increment in concentration occurs for Soret number.
- Reverse trend in solutal transport rate is noticed for random (Nb) and thermophoresis (Nt) variables.
- Soret number variation decays mass transport rate.
- Peclet number leads to intensifies the microorganism density number, while opposite trend seen for microorganism field.
- Microorganisms field decays for larger bioconvection Lewis number,
- An increase in microorganism density number is detected for higher bioconvection (Lb) Lewis number.

Author contributions

All authors are equally contributed in the research work.

Declaration of competing interest

The authors declared that they have no conflict of interest and the paper presents their own work which does not been infringe any third-party rights, especially authorship of any part of the article is an original contribution, not published before and not being under consideration for publication elsewhere.

Data availability

No data was used for the research described in the article.

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