

Effect of fracture roughness on the hydrodynamics of proppant transport in hydraulic fractures.

SURI, Y. ISLAM, S.Z. and HOSSAIN, M.

2020



Effect of Fracture Roughness on the hydrodynamics of proppant transport in hydraulic fractures

Yatin Suri, Sheikh Zahidul Islam*, and Mamdud Hossain
School of Engineering, Robert Gordon University, Aberdeen, AB10 7GJ, UK

*Corresponding author. Email: s.z.islam1@rgu.ac.uk

Phone: +44(0)1224 262319

Fax: +44(0)1224 262444

Abstract-

The effect of fracture roughness is investigated on proppant transport in hydraulic fractures using Joint Roughness Coefficient and a three-dimensional multiphase modelling approach. The equations governing the proppant transport physics in the fracturing fluid is solved using the hybrid computational fluid dynamics model. The reported proppant transport models in the literature are limited to the assumption of a smooth fracture domain with no fluid leak-off or fluid flow from fracture to rock matrix interface. In this paper, a proppant transport model is proposed that accounts for the proppant distribution in rough fracture geometry with fluid leak-off effect to surrounding porous rock. The hydrodynamic and mechanical behaviour of proppant transport was found directly related to the fracture roughness and flow regime especially under the influence of low viscosity fracturing fluid typically used in shale gas reservoirs. For the proppant transport in smooth fractures, the fracture walls employ mechanical retardation effects and reduce the proppant horizontal velocity resulting in more significant proppant deposition. On the contrary, for the proppant transport in rough fractures, the inter-proppant and proppant wall interactions become dominant that adds turbulence to the flow. It results in mechanical interaction flow effects becoming dominant and consequently higher proppants suspended in the slurry and greater horizontal transport velocity. Furthermore, the mechanical interaction flow effects were found to be principally dependant on the proppant transport regime and become significant at higher proppant Reynolds number.

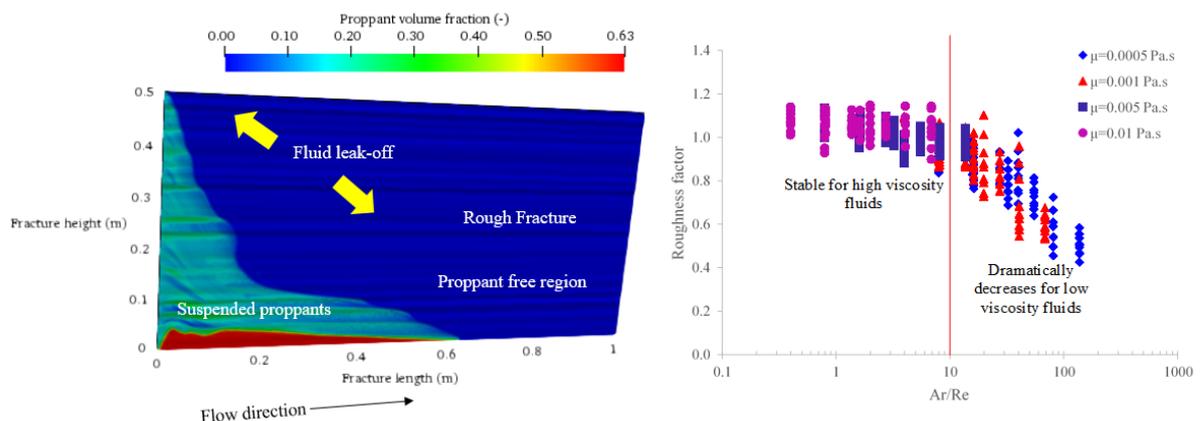
Keywords

Joint roughness coefficient; Computational Fluid Dynamics; Hydraulic fracturing; Fluid Leak-off; Proppant transport; Fracture Roughness

Highlights

- Effect of fracture roughness investigated on proppant transport and distribution
- Fracture roughness modelled using Joint Roughness Coefficient (JRC)
- Mechanical interaction effects become dominant at higher JRC and Reynolds number

Graphical abstract



41
42

1. Introduction-

Solid transport with fluid in the form of slurry flow is widespread in several diverse applications, like sand transport in the river, wastewater disposal, petroleum engineering or proppant transport during hydraulic fracturing, and fluidized-bed reactors (Chalov et al., 2015; Sahu et al., 2013; Tong and Mohanty, 2016). In all the applications, the discrete phase, i.e. solid, is suspended in the continuous phase, i.e. fluid, and frequent momentum transfer occurs between both the phases (Dontsov and Peirce, 2014). The three critical physical phenomena that affect the hydrodynamics of particle transport in the fluid are a fluid drag, particle settlement and particle-wall interaction (Patankar and Joseph, 2001). The continuous phase exerts a drag force on the particles and changes the particle transport velocity. Due to the drag force and the energy dissipation, the particle travels slowly compared to the fluid, and this results in slippage velocity (Zhang et al., 2017). This particle-fluid coupling adds complexity to the flow. In addition, based on the concentration of the suspended particles, the inter-particle collision can significantly affect the transport phenomenon (Blyton et al., 2015). The higher inter-particle collision can be dominant in the dense phase transport that increases the randomness and turbulence in the flow adding further complexity (Blyton et al., 2015). Lastly, for the slurry flow in rough wall surfaces, the irregular wall results in higher particle-wall interactions and significantly increases the flow disturbance affecting the hydrodynamic and mechanical properties of solid transport (Zhang et al., 2019b). Zhang et al. (2019a) comprehensively investigated the effect of 2D rough fractures on single-phase fluid flow and microflow effects, i.e. when the fracture aperture approaches the mean free path of fluid molecules. It was proposed that the fracture roughness significantly alters the relationship between the hydraulic and mechanical apertures, which further affects the velocity and pressure fields inside the fracture.

In the petroleum industry, hydraulic fracturing is one of the widely used technology for hydrocarbon production, particularly in shale gas reservoirs (Veatch et al., 2017). The process of hydraulic fracturing includes injection of high-pressure fluid (or fracturing fluid) into the subsurface rock through the wellbore, to create fractures or cracks (Uddameri et al., 2015). The purpose of these fractures is to provide a conductive path for the hydrocarbons to enter the wellbore or to increase the connectivity of the existing fractures (Speight, 2016). Post creation of the fractures, solid particles like sand are dispersed in fluid, and the slurry is injected. The solid particles are known as proppants. The key role of injecting proppants is firstly to prevent the fracture from closing when the hydraulic pressure is removed, and secondly to provide the adequate flow conductivity from the tight reservoir to the wellbore (Smith and Montgomery, 2015). Particularly, in shale gas reservoirs, the slick water fracturing fluid is most commonly used for conducting hydraulic fracturing (Suri et al., 2019). Due to the low viscosity of the slick water fracturing fluid, it possesses a poor ability to suspend proppants (Sahai et al., 2014). The productivity of the hydraulically fractured wells is dependent on the propped fractures, which is driven by the proppant settlement and transport inside the fractures (Bokane et al., 2014). Typically, the fracture aperture is around 3 mm – 10 mm. During the transport of the fracturing fluid slurry suspended with proppants in the narrow fracture opening, the fracture walls exert a mechanically induced flow effect that influences the proppant transport velocity and proppant settlement (Zhang et al., 2019b). Thus, the frequent proppant-fluid, inter-proppant and proppant-rough wall interactions lead to a complex proppant transport physics in fracturing fluid flow. This complex phenomenon leads to the current study of fracture roughness in the proppant transport model appealing to petroleum engineers and researchers (Deshpande et al., 2013).

Particles settling in cylinder tubes have frequently been investigated (Arsenijević et al., 2010; Chhabra et al., 2003; Delidis and Stamatoudis, 2009). The wall factor, which is the ratio of the particle terminal velocities in bounded and unbounded fluids, is typically defined to determine the hydrodynamic drag force on particles. From the literature, it is recognised that the wall factor for spheres settling in a fluid is mainly dependant on the size ratio of the sphere diameter

98 to the inner tube diameter and the Reynolds number. Recently, Malhotra and Sharma (2012)
99 and Zhang et al. (2016) investigated the settling velocity of spherical particles between two
100 parallel plates for Newtonian and non-Newtonian fluids. However, the surface of the plates was
101 assumed as smooth, and no effect of fracture roughness was studied.

102
103 The multiphase flow of fracturing fluid and proppants in the hydraulic fracture can be
104 categorised into three regions contingent on the inter-proppant association: negligible collision
105 flow, predominant collision flow and predominant contact flow. In the region where the flow
106 is predominantly governed by collision, the interaction between proppant-fluid, proppant-
107 proppant and proppant-rough fracture wall need to be accurately modelled.

108 To numerically simulate the multiphase slurry flow where the solid particles are suspended in
109 the fluid is mainly modelled using following two numerical modelling techniques. Firstly, the
110 Eulerian-Lagrangian technique tracks the trajectory of individual particles and models
111 accurately the inter-proppant interaction or collision, and proppant-wall interaction. Secondly,
112 the Eulerian-Granular method models the average behaviour of proppants and calculates overall
113 diffusion and convection of a group of proppants based on empirical relationships or kinetic
114 theory of granular flow. The computational time required for solving the proppant transport
115 physics using the Eulerian-Lagrangian method is substantially higher as it tracks the motion of
116 individual particles, and thus this method is less appealing for simulating field scale fractures.
117 In the current study, a hybrid model is used (Suri et al., 2019), which tracks the trajectory of
118 individual proppants based on Eulerian-Lagrangian method, but models the proppant-fluid and
119 inter-proppant physics using the kinetic theory of granular flow based on Eulerian Granular
120 method. The method is computationally less expensive compared to Eulerian-Lagrangian
121 method and captures the hydrodynamics of proppant transport accurately.

122
123 The hydrodynamics of proppant transport in fractures is a complex process, and the factors like
124 fracture geometry, fracture roughness, and fluid leak-off add additional challenges to model the
125 flow phenomenon numerically. In recent years, several researchers have modelled the proppant
126 transport physics in hydraulic fractures using computational fluid dynamics (CFD) technique.
127 Zhang and Dunn-Norman (2015) examined the proppant distribution at different perforation
128 angle in fractures or the inclination at which the fractures were created and compared the
129 pressure drop using CFD. Kou et al. (2018) investigated the proppant transport and distribution
130 in the hydraulic fracture and natural fracture intersection using the discrete element method
131 (CFD-DEM model). Hu et al. (2018) proposed an idea of using Eulerian-Eulerian proppant
132 transport model for field-scale hydraulic fractures using dimension reduction strategy. The
133 reported studies are limited to the assumption of smooth planar fracture geometry with no leak-
134 off effects from the fracture wall. The fracture roughness coupled with fluid leak-off can
135 significantly impact the proppant transport physics. Zhang et al. (2019b) investigated the Joint
136 Roughness Coefficient (JRC) fracture profiles and proposed a proppant transport model in
137 rough fractures. However, the model is limited to two-dimensional fracture geometry, and
138 gravitational effects along with fluid-leak off effects were ignored. The existing proppant
139 transport models are limited to modelling proppant hydrodynamics in smooth two-dimensional
140 fracture geometry with no fluid leak-off from the fracture to the surrounding reservoir. Barton
141 and Choubey (1977) proposed the joint roughness coefficient to characterise fracture roughness
142 and predict the shear strength of different rock type. In the current study, the approach used by
143 Barton and Choubey (1977) of joint roughness coefficient is further developed to investigate
144 its effect on the fluid flow and proppant hydrodynamics comprehensively. A three-dimensional
145 proppant transport model is proposed that accurately models the proppant transport physics in
146 rough fractures and successfully configures the fluid flow from fracture sidewall to surrounding
147 porous rock. The rough fracture profiles are created using the JRC described later in section
148 2.1. Subsequently, the dimensional analysis is carried out to identify the relationship between
149 the critical dimensionless flow parameters and proppant transport regime. It is followed by a
150 comparison of the proposed hybrid model against the published experimental results. Lastly, a
151 comprehensive investigation of proppant transport in smooth and rough fractures with
152 dimensionless parameters is presented.

2. Model development-

The principal aim of the present work is to extensively investigate the impact of fracture roughness on the hydrodynamics of proppant transport during hydraulic fracturing. A hybrid (CFD-DEM) numerical model is used to solve this multiphase flow problem in rough fracture profiles coupled with the effect of fluid leak-off from the fracture wall.

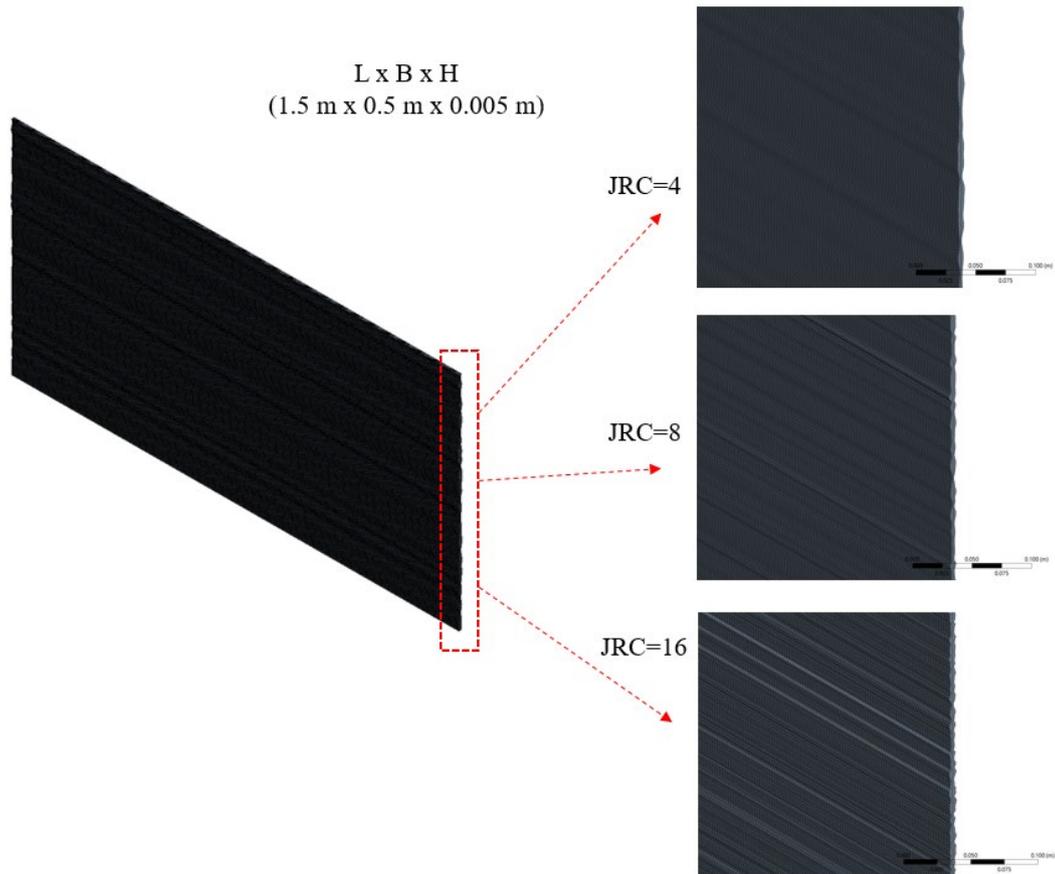
2.1. Problem formulation and Joint Roughness Coefficient profiles

Barton and Choubey (1977) were among the early researchers who studied the fracture roughness in detail and proposed a parameter called Joint Roughness Coefficient (JRC), denoted by Θ_{JRC} , to differentiate the rough fractures. The equation for JRC is defined by Eq. (1)

$$\Theta_{JRC} = \frac{\tan^{-1}\left(\frac{\tau}{\sigma_n}\right) - \Phi_b}{\log\left(\frac{\sigma_c}{\sigma_n}\right)} \quad (1)$$

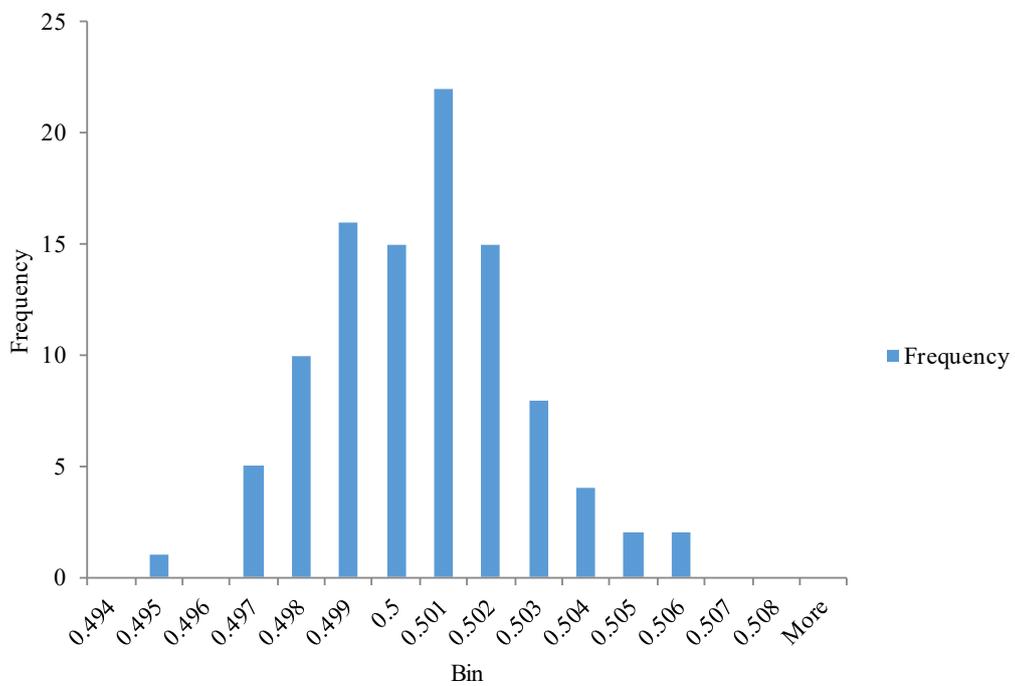
Where τ is the maximum shear strength; σ_n is the effective stress in the normal direction; Φ_b is the angle of friction; and σ_c is fracture compressive strength. Barton and Choubey (1977) calculated the value of JRC for different rock types. The JRC value for calcareous shale was calculated as 8.2. More recently, Kassis and Sondergeld (2010) extracted the SEM image of a Barnett shale core sample in order to investigate the fracture roughness. The fracture roughness for the Barnett shale sample can be related to the JRC scale of Barton and Choubey (1977) in between 10-11. Furthermore, some of the smooth rock types analysed by Barton and Choubey (1977) are Slate and Gneiss whose JRC values range in between 2-6. The fracture profiles with different JRC values are shown in Fig. 1.

In the present study, three different rough fracture profiles were created with JRC values 4, 8 and 16 using the published data by Barton and Choubey (1977) and the fractal theory proposed by Mandelbrot (1983). The fractal theory helps in characterising the randomly distributed irregular fracture surfaces resulting in fracture roughness with different JRC values (Alves, 2012). The rough fracture profiles were created based on the methodology from Briggs et al. (2017) and SynFrac software (Ogilvie et al., 2006). The JRC fracture profiles are displayed in Fig. 1 and are constructed such that the fracture aperture followed a normalised distribution curve shown in Fig. 2 with a mean aperture of 5 mm and a standard deviation of 0.1 mm. The fracture domain in the present study has length 1.5 m, aperture 5 mm and height 0.5 m. In the present study, no dynamic fracture propagation is assumed.



188
189
190

Fig. 1. Rough fracture geometries with different JRC values



191
192
193
194

Fig. 2. Normal distribution curve to create a rough fracture profile

2.2. Mathematical model

2.2.1. Governing Equations

As discussed earlier, the multiphase flow of fluid with suspended proppants can be numerically modelled using mainly two methods- Eulerian-Granular method and Eulerian-Lagrangian method (or Discrete Element method). In order to take advantage of both these methods, a hybrid model is used in the current study that tracks the trajectory of individual proppants using Eulerian-Lagrangian approach with the fluid-proppant and inter-proppant interactions modelled using the kinetic theory of granular flow from Eulerian-Granular method. The equations describing the hybrid model for proppant transport used in the current study are explained in detail in our previous work (Suri et al., 2019). However, the key governing equations are briefly described as follows-

The mass and momentum conservation equations are given by Eq. (2) and Eq. (3):

$$\rho_i \left(\frac{\partial}{\partial t} \alpha_i + \nabla \cdot \alpha_i \vec{v}_i \right) = S_m \quad (2)$$

$$\frac{\partial}{\partial t} (\alpha_i \rho_i \vec{v}_i) + \nabla \cdot (\alpha_i \rho_i \vec{v}_i \vec{v}_i) = -\alpha_i \nabla p + \nabla \cdot \bar{\bar{\tau}}_i + \alpha_i \rho_i g + \bar{\bar{M}}_{is} + S_u \quad (3)$$

Where α is the phase volume fraction, S_m and S_u are mass and momentum source term respectively, $\bar{\bar{\tau}}_i$ and $\bar{\bar{M}}_{is}$ are the tensor variable of stress-strain for fluid phase and momentum exchange term, respectively. ρ , v , g are the density, velocity, and acceleration due to gravity respectively.

The trajectory of the proppant phase can be calculated based on Eq. (4)

$$\frac{d\vec{v}_p}{dt} = \frac{\vec{v}_i - \vec{v}_p}{\tau_r} + \frac{g(\rho_p - \rho)}{\rho_p} + \bar{\bar{F}}_{KTGF} \quad (4)$$

In the right-hand side of Eq. (4), the first term refers to drag force, the central term refers to the gravity force and the last term the force due to kinetic theory of granular flow. The velocity and hence the location of proppant phase can be calculated using Eq. (4) at every time step. The detailed definition of the variables used in Eq. (4), the constitutive relationships for fluid-proppant and inter-proppant interactions, and the drag model can be found in Suri et al. (2019).

2.2.2. Physical model

The effect of fracture roughness on proppant transport in hydraulic fracture was investigated using the CFD technique in ANSYS FLUENT. The geometry or computational domain used in the current study is, as shown in Fig. 1 and Fig 3. The slurry of proppants suspended in the water is injected with a specified velocity inlet boundary condition. In the real hydraulic fractures which are surrounded by the porous rock, the fluid after entering into the fracture domain leaks into the surrounding reservoir rock. The amount of leakage depends upon the reservoir characteristics such as reservoir porosity and permeability. To evaluate the amount of fluid leakage from the fracture-matrix interface, an explicit CFD study with reservoir porosity 5% and reservoir permeability 0.5 mD is conducted. The fluid leak-off profile obtained from the analysis is detailed in Fig. 4. The leak-off profile from Fig. 4 is used to write a code in C++ and configure into the CFD solver. The key role of the code is to add source terms into the continuity and momentum conservation equations so that a particular amount of fluid at the fracture wall is lost at every simulation time step. The detailed understanding of the underlying equations describing the source terms and code used to incorporate the effect of dynamic fluid leak-off in proppant transport model is explained in our previous work (Suri et al., 2019).

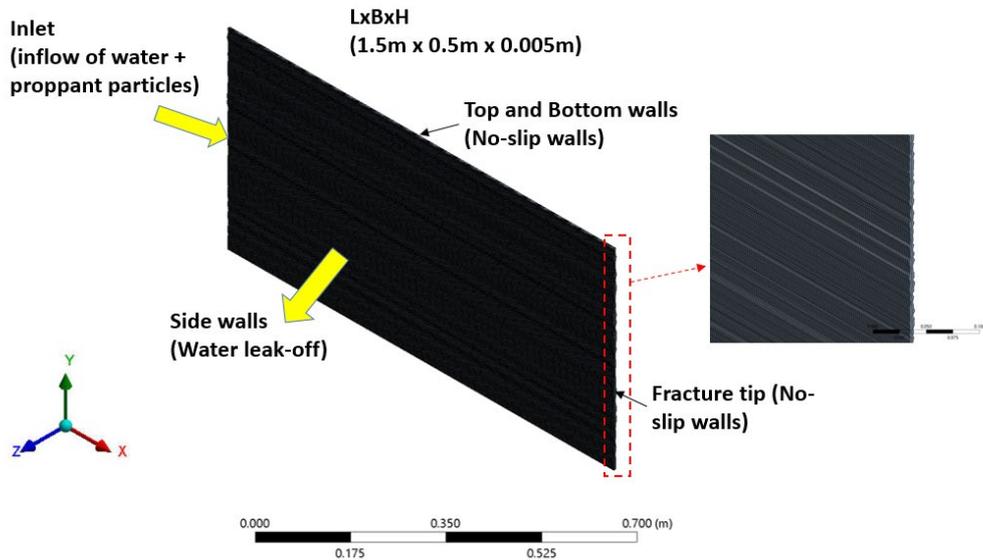


Fig 3. Computational domain

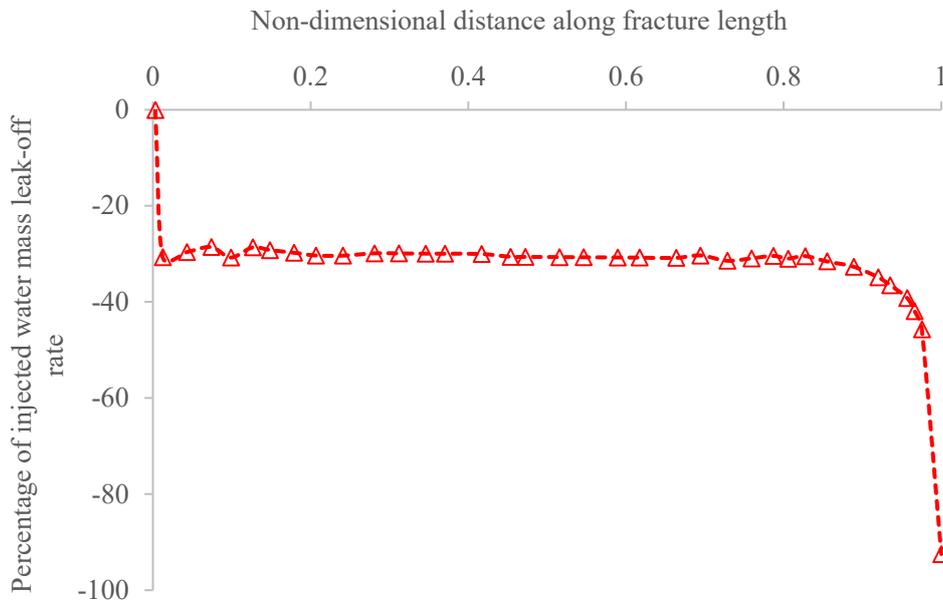


Fig. 4. Amount of fluid leakage at the fracture-matrix interface

240
241

242

243
244

245

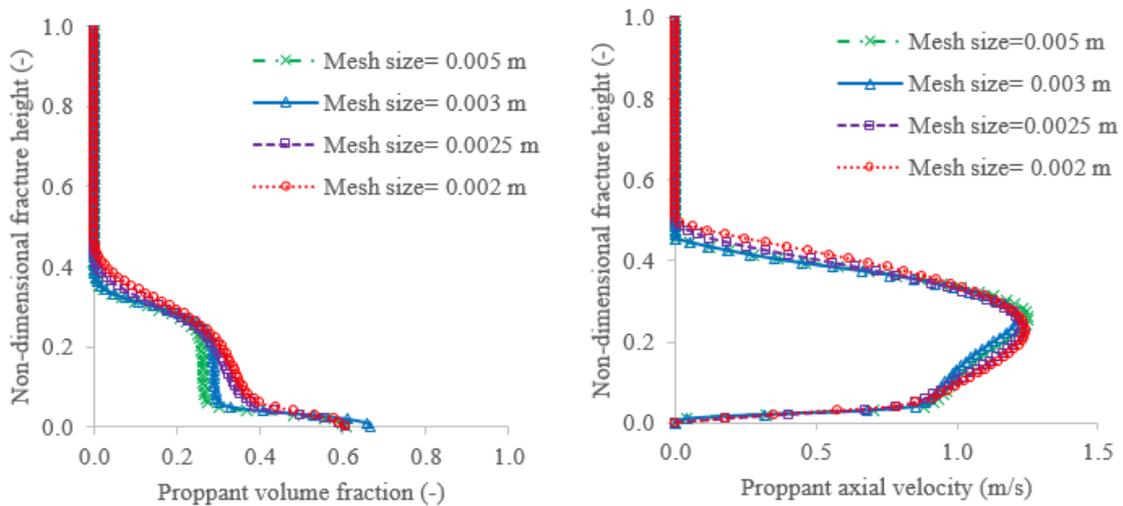
246 Next, to investigate in detail the effect of fracture roughness in proppant transport regime,
 247 different proppant and fluid properties are varied one at a time and simulation run with proposed
 248 proppant transport model is performed. The key parameters that were varied include proppant
 249 size, the injection rate (or injection velocity), fluid viscosity and fracture width for different
 250 JRC fracture profiles, as shown in Table 1. The density of proppants and fluid used in the
 251 present study is 2650 kg/m³ and 1000 kg/m³, and the volume fraction of proppants in the slurry
 252 was used as 15 %. The key CFD modelling specific parameters used in the current model are
 253 explained in detail in our previous work (Suri et al., 2019).

254
255
256

257 **Table 1**
 258 Key modelling parameters

Properties	Value
Proppant diameter	0.35, 0.50, 0.65 mm
Fluid inlet velocity	0.1, 0.25, 0.5 m/s
Fluid viscosity	0.0005, 0.001, 0.005, 0.010 Pa-s
Fracture width	3, 5, 10 mm
JRC	0 (Smooth), 4, 8, 16

259
 260 A mesh sensitivity analysis was conducted such that the solution is independent of the mesh.
 261 Proppant volume fraction and axial velocity were compared with different mesh sizing
 262 parameters against fracture height at a cross-section plane at 0.5 m from the inlet and detailed
 263 in Fig. 5. The results from the mesh sensitivity study, suggest that the mesh size of 0.0025 m
 264 provides the computationally efficient and mesh independent solution with (600×200×2
 265 elements).
 266
 267



268
 269 **Fig. 5. Mesh Sensitivity Study**

270 2.3. Dimensional analysis

271 Non-dimensional parameters used in the present study were derived using the dimensional
 272 analysis as proposed in Tan (2011). The key parameters that affect the proppant transport and
 273 fluid flow in hydraulic fractures are- Proppant properties (proppant size or proppant diameter
 274 d_p , proppant density ρ_p), fracturing fluid properties (fluid viscosity μ_i , fluid density ρ_l ,
 275 injection flow rate or injection velocity v_i), geo-mechanical parameters (fracture width w ,
 276 fracture roughness Θ_{JRC} , fluid leak-off rate c_L) (Li et al., 2018). Thus, the proppant distribution,
 277 pressure and velocity as a function of flow properties can be written as:

278 $(\alpha, v, P) = f(d_p, \rho_p, \rho_l, v_i, \mu_i, w, c_L, \Theta_{JRC})$ (5)

279 Eq. (5) can be written in the non-dimensional form by using proppant diameter d_p , injection
 280 velocity v_i and fracturing fluid density ρ_l

281
 282 $(\alpha, \frac{v}{v_i}, \frac{P}{\rho_l v_i^2}) = f(\frac{d_p}{w}, \frac{\rho_p}{\rho_l}, \frac{v_s}{v_r}, \frac{\rho_l v_i d_p}{\mu_i}, \frac{(\rho_p - \rho_l) \rho_l d_p^3 g}{\mu_i^2}, c_L, \Theta_{JRC})$ (6)
 283

284 Where, $\frac{\rho_l v_i d_p}{\mu_i}$ refers to the fraction of inertial force to viscous effects and represents the
 285 Reynolds number; and $\frac{(\rho_p - \rho_l) \rho_l d_p^3 g}{\mu_i^2}$ is the Archimedes number that describes the ratio of inertia
 286 effects to gravity effects.

287
 288 The density ratio of proppant-to-fluid is constant, and the leak-off rate depends on the reservoir
 289 characteristics (porosity and permeability), which are also assumed as constant for a given
 290 porosity and permeability. Therefore, Eq. (6) can be re-written as-

$$291 \left(\alpha, \frac{v}{v_i}, \frac{P}{\rho_l v_i^2} \right) = f \left(\frac{d_p}{w}, \frac{v_s}{v_r}, Re, Ar, \Theta_{JRC} \right) \quad (7)$$

292
 293 A series of simulation was performed by varying the injection velocity, proppant diameter, fluid
 294 viscosity, and fracture roughness one at a time. A detailed investigation of the role of the non-
 295 dimensional parameters on the proppant transport characteristics was carried out and explained
 296 in the following section.

297

298 3. Results and Discussion-

299

300 3.1. Comparison with the experimental results-

301 Tong and Mohanty (2016) performed an experimental study of proppant transport in fracture
 302 slots at different injection rates, which was used to compare the numerical results from the
 303 present hybrid proppant transport model. The experiment consisted of two transparent fracture
 304 slots, as shown in Fig. 6 at different bypass angles. The two different fracture slots represent
 305 the interactions between hydraulic fracture and natural fracture. The main fracture slot is called
 306 as a primary fracture slot and the bypass fracture slot is called as a secondary fracture slot. The
 307 dimensions of the primary fracture slot were 0.381 m × 0.002 m × 0.0762 m in L×W×H, and
 308 the secondary slot were 0.1905 m × 0.002 m × 0.0762 m in L×W×H. The slick water slurry
 309 with the suspended proppants is injected using a progressive cavity pump and sand funnel
 310 through the inlet located at the right end of the main fracture slot, as shown in Fig. 6. The
 311 fracturing fluid slurry (water + proppants) is injected at the inlet at different flow rates or
 312 injection velocities (0.1, 0.2 and 0.3 m/s) and proppant concentration (0.038, 0.019, and 0.013).
 313 20/40 size sand is used as a proppant with a density of 2650 kg/m³. Water is used as a fracturing
 314 fluid with viscosity 1 cP and density 1000 kg/m³. The proppant transport was monitored and
 315 recorded with cameras as shown in Fig. 6. The proppant bed deposition after 40 s of injection
 316 for different flow rates (or injection velocities) is compared for both the numerical and
 317 experimental results and are shown in Fig. 7. For quantitative comparison, the fraction of
 318 proppant deposited in the secondary fracture slot over the primary fracture slot was calculated
 319 and plotted at different injection velocities for both, experimental and simulation results, as
 320 shown in Fig. 8. The comparison of results in Fig. 7 and Fig. 8 suggests a reasonable match
 321 between the numerical simulation and experiment with a percentage error of 3.2% and 3% for
 322 proppant bed height and length, respectively.

323 The results suggest an overall good match between the numerical model and experiment, and
 324 the model can be used for the detailed investigation of the effect of fracture roughness in the
 325 hydrodynamics of proppant transport.

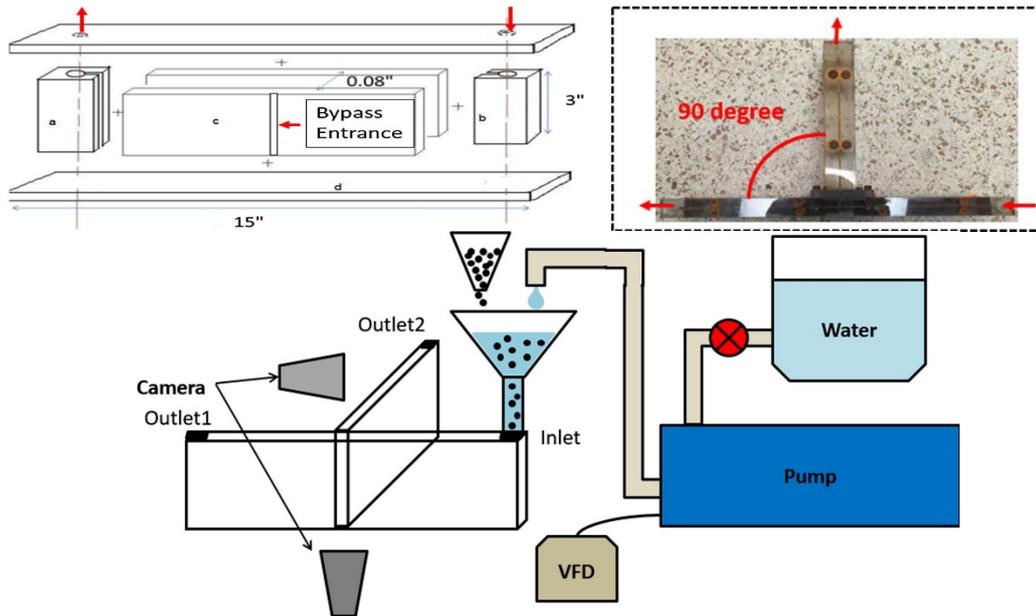
326

327

328

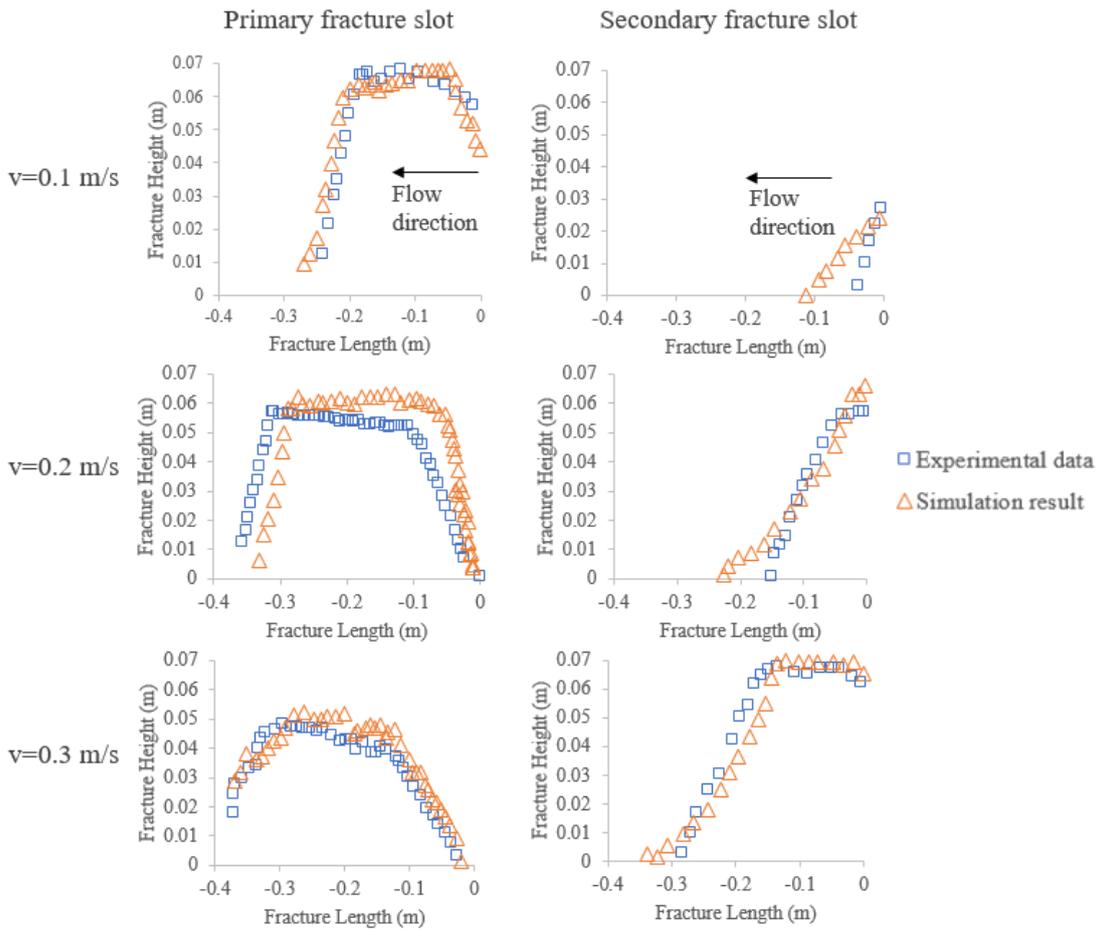
329

330



331 **Fig. 6.** Schematic of the proppant transport fracture slot experiment (Tong and Mohanty,
 332 2016)

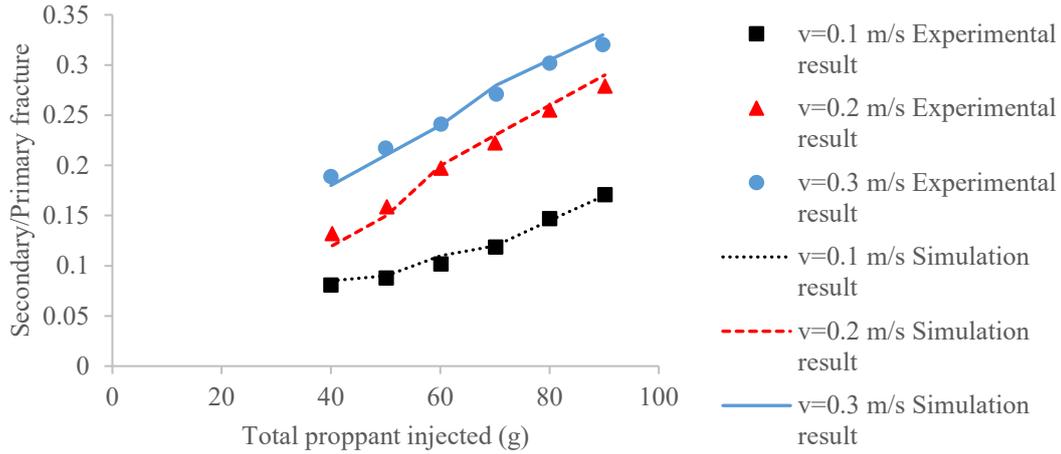
333



334
 335

Fig. 7. Comparison of proppant bed deposition at $t=40$ s

336

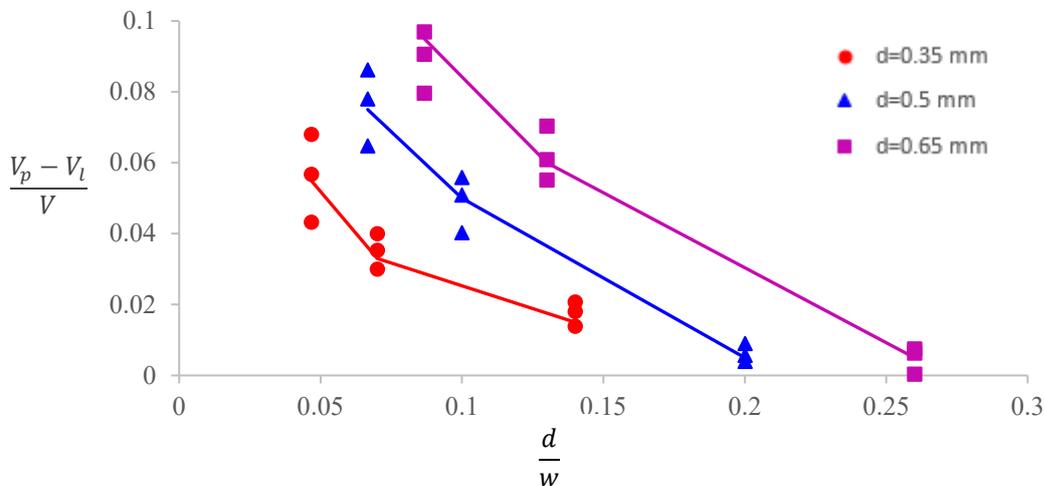


337
338 **Fig. 8.** Quantitative comparison of results – a fraction of proppant deposited in
339 secondary/primary fracture slot at different injection velocities

340 *3.2. Proppant transport and distribution in smooth fracture*

341
342 In the slurry flow, the fracturing fluid carries the proppants inside the fracture, and the fracturing
343 fluid also exerts a drag force on the proppants. Due to the drag force and the energy dissipation,
344 the proppant travels slowly compared to the fluid, and this results in slippage velocity. The
345 proppant motion with fluid can be characterised by the slippage velocity, which is a difference
346 in the fluid and proppant velocity. The slippage velocity depends upon the proppant size and
347 fracturing fluid rheology. Furthermore, when the proppant transport in the hydraulic fractures,
348 the interaction between the proppants and fracture wall affects the horizontal motion. The flow
349 velocity at the centre of the fracture is highest resulting in proppants to transport faster and is
350 smallest near the walls due to non-slip walls, and high shear-induced forces.

351 To understand the effect of slippage velocity and proppant size ratio on proppant transport, a
352 normalised graph is plotted against variables $\frac{V_p - V_l}{V}$ and $\frac{d}{w}$ as shown in Fig. 9. Where, $V_p - V_l$
353 represents the slippage velocity, V is the characteristic velocity and can be defined by \sqrt{gd} , d
354 is the proppant diameter and w is the fracture width. It can be interpreted from the figure that
355 as the fracture width decreases or proppant diameter increases, the size ratio $\left(\frac{d}{w}\right)$ increases. It
356 results in greater fracture wall retardation effect on proppant motion and consequently decrease
357 in the proppant horizontal transport velocity or slippage velocity.
358

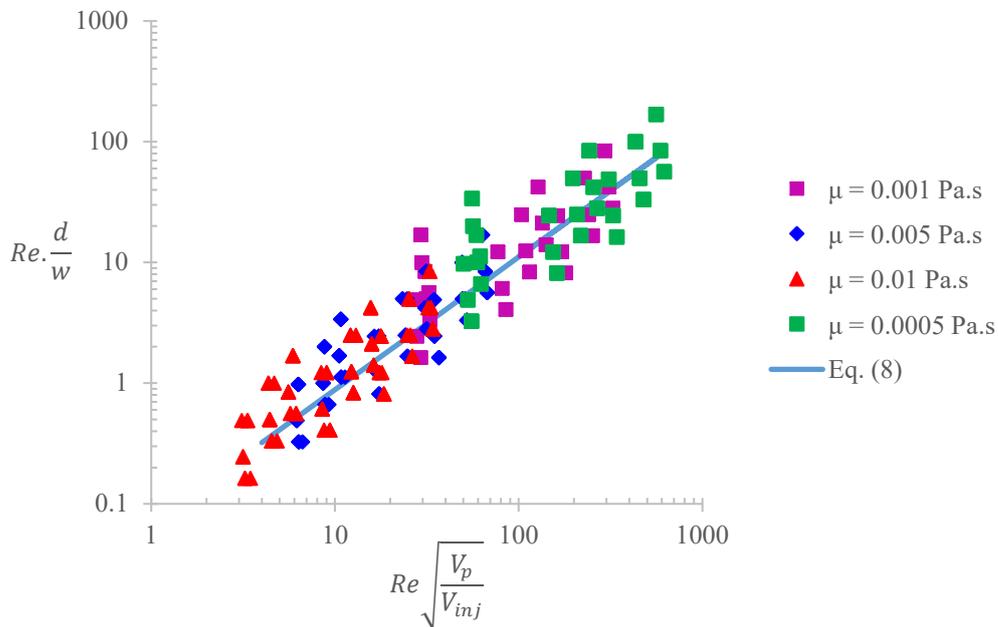


359
360 **Fig. 9.** Variation of slippage velocity with proppant size ratio
361
362

363 The slippage velocity depends on the injection velocity, proppant size and proppant Reynolds
 364 number. Thus, to understand the role of slippage velocity on proppant and fluid properties, two
 365 non-dimensional variables were evaluated $Re \cdot \frac{d}{w}$ and $Re \sqrt{\frac{V_p}{V_{inj}}}$. $Re \cdot \frac{d}{w}$ is a function of proppant
 366 size and $Re \sqrt{\frac{V_p}{V_{inj}}}$ depends on the slippage velocity. The simulation results of all the cases in
 367 Table 1 with a smooth fracture profile are plotted on a log-log scale in Fig. 10. It can be
 368 interpreted that $Re \cdot \frac{d}{w}$ and $Re \sqrt{\frac{V_p}{V_{inj}}}$ varies linearly in a log-log scale and the power law
 369 correlation was defined using the curve fitting, which can be directly used in the fracture
 370 simulators to determine the average horizontal velocity of proppants in smooth fractures.
 371

$$372 \quad Re \cdot \frac{d}{w} = 0.07 \left(Re \sqrt{\frac{V_p}{V_{inj}}} \right)^{1.1} \quad (8)$$

373 Where V_{inj} is the injection velocity in m/s.
 374



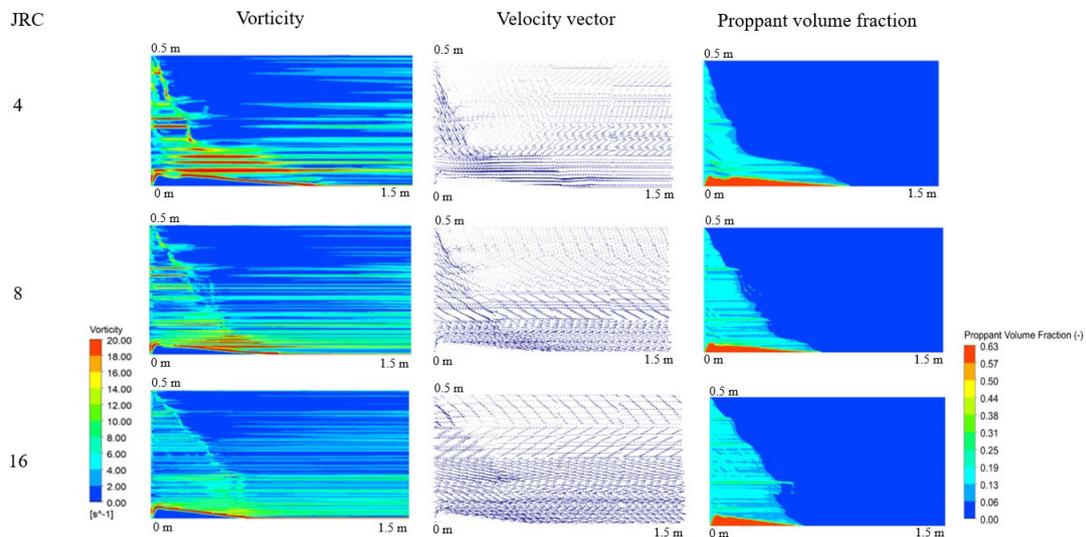
375
 376
 377
 378 **Fig. 10.** Log-log plot of correlation between proppant Reynolds number, proppant size ratio
 379 and proppant horizontal velocity in smooth fracture

380 381 3.3. Role of fractures roughness on proppant hydrodynamics 382

383 The fracture roughness or the irregular wall surfaces can aid in greater inter-proppant
 384 interactions and proppant-fracture wall interaction, which consequently influence the proppant
 385 transport and distribution. In order to investigate in detail, the role of fracture roughness in
 386 proppant transport regime, understanding of the different fracture roughness and flow
 387 parameters is prerequisite. As mentioned earlier, Barton and Choubey (1977) were among the
 388 early researchers who studied the fracture roughness in detail and proposed a parameter called
 389 Joint Roughness Coefficient to differentiate different rough fractures. The equation for JRC is
 390 defined in Eq. (1). In the present study, the rough fractures were created using the JRC profiles
 391 from the study of Barton and Choubey (1977) using different JRC profiles and SynFrac
 392 software as described earlier. However, the fracture geometries using JRC profiles were created
 393 such that it followed a normalised distribution with a mean aperture equal to fracture width.
 394 Then the proppant transport was modelled in the rough fractures using the hybrid model (CFD-
 395 DEM) described earlier, and the simulation results in the form of contour plots are shown in

396 Fig. 11. The results in Fig. 11 suggest that fracture roughness plays a significant role in proppant
 397 transport. As the JRC increases, it escalates the inter-proppant and proppant-fracture wall
 398 interaction. Consequently, it adds that the degree of randomness in the flow to make it more
 399 turbulent and complex.

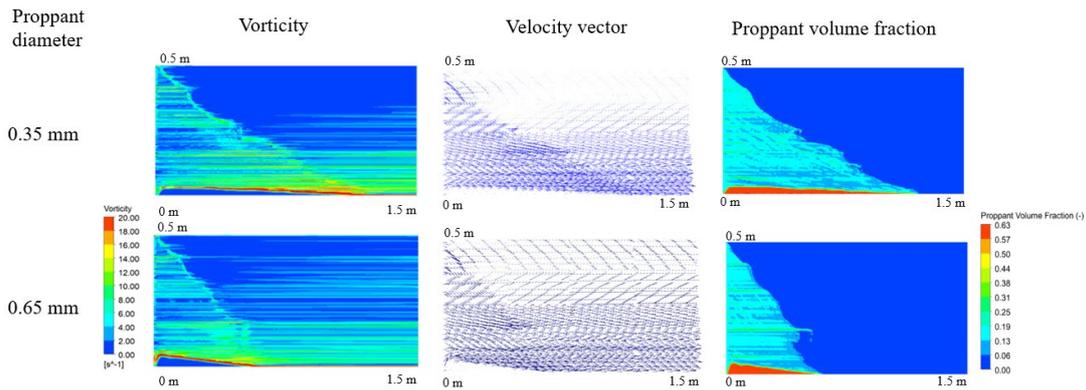
400
 401 The fracture roughness further affects the hydrodynamic and mechanical behaviours of the
 402 proppant flow. The turbulence in the flow due to the fracture roughness increases the ability of
 403 proppants to suspend in the fluid and support the proppant to transport longer distance into the
 404 fracture. Fig. 11 shows the comparison of vorticity, velocity vector plot and proppant volume
 405 fraction plot for different JRC fracture profiles. It can be interpreted from the comparison that
 406 with the increase in JRC, it increases the vorticity in the flow due to higher turbulence and flow
 407 instability caused by the proppant-wall and inter-proppant collisions. Notably, at the fracture
 408 wall, the high vortex region is evident where the proppant frequently collides with the rough
 409 fractures leading to higher turbulent kinetic energy and randomness in the flow. This roughness
 410 induced turbulence is also evident in the velocity vector plot for different JRC profiles. On
 411 comparison of proppant volume fraction contour plot for different JRC profiles, two important
 412 observations can be noticed. Firstly, with the increase in JRC value, the increase in the amount
 413 of proppant suspension is evident in Fig. 11 by the size of the proppant suspension layer. This
 414 suggests that with time, the suspended proppant can be transported further inside the fracture.
 415 Thus, neglecting the JRC or effect of fracture roughness could lead to inaccurate estimation of
 416 the proppant and fluid velocity into the hydraulic fracturing design. Secondly, for the lower
 417 value of JRC or relatively smooth fractures, the fracture wall exerts an additional force or
 418 mechanical retardation force on proppants, which slows down the suspended proppants and
 419 results in more proppant deposition. This is evident in Fig. 11, where the proppant bed observed
 420 in JRC 4 is greater than JRC 8 and JRC 16 fracture profiles. The mechanical retardation effect
 421 becomes more dominant, especially in the low viscosity fracturing fluid, like slick water,
 422 commonly used in shale gas reservoirs. In the high viscosity fracturing fluid, the effect is less
 423 dominant.
 424



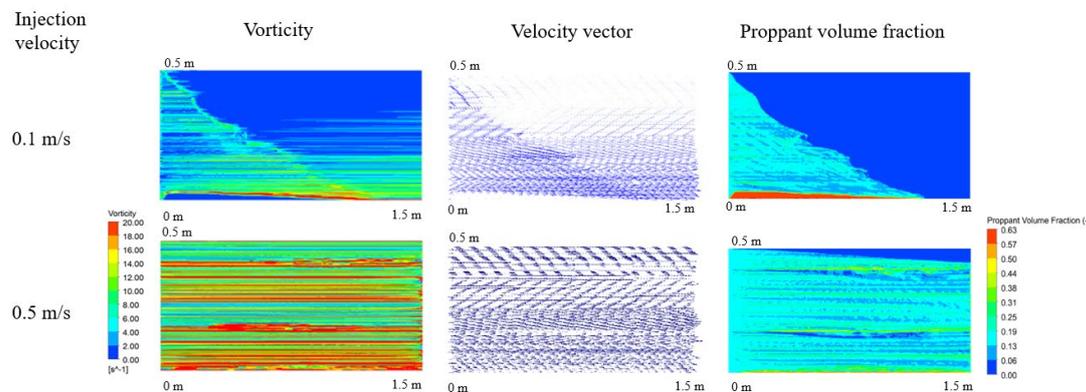
425
 426 **Fig. 11.** Comparison of vorticity, velocity vector and proppant volume fraction for different
 427 JRC profiles
 428

429 Next, to investigate the impact of fractures with different JRC profiles on flow regimes, the
 430 proppant size and injection rate were varied and compared in Fig. 12 and Fig. 13 respectively.
 431 It can be interpreted from Fig. 12 proppant volume fraction plots that proppant particles with
 432 greater size form a larger proppant bed compared to smaller size proppants. On the contrary, in
 433 terms of proppant suspension, the proppants with smaller size is noted to have a larger
 434 suspension region in Fig. 12 proppant volume fraction plot compared to the larger size

435 proppants. This can be explained by the proppants with greater size due to its comparatively
 436 heavier weight has a higher vertical settling velocity and thus greater tendency to deposit.
 437 Conversely, the smaller size proppants due to the lower settling velocity is easily carried away
 438 by the flowing fluid and thus resulting in more suspended proppant particles.
 439 Fig. 12 shows that as the injection rate or injection velocity is increased, less proppant
 440 deposition is seen in the volume fraction contour plot. This can be explained by the increase in
 441 injection velocity results in the increase in the ability of the proppants to suspend and creates
 442 randomness in the flow. This further leads to high vorticity in the flow. Thus, a higher number
 443 of suspended proppants due to increase in injection velocity can aid in more extended proppant
 444 transport.
 445



446 **Fig. 12.** Comparison of proppant transport in rough fractures with proppant diameter 0.35 mm
 447 and 0.65 mm
 448
 449



450 **Fig. 13.** Comparison of proppant transport in rough fractures with different flow injection
 451 velocities
 452
 453

454 Next, a comparison is made between proppant transport in smooth and rough fracture case with
 455 JRC of 16, proppant diameter of 0.65 mm, fluid viscosity of 1 cP and injection velocity of 0.1
 456 m/s. As explained earlier, it is evident from Fig. 13 that due to the rough fracture wall, the
 457 mechanical interaction between the proppant-fracture wall increases and it significantly impacts
 458 the vorticity and turbulence in the flow. The increase in the vorticity leads to the higher ability
 459 of the slurry to suspend proppants and consequently less deposition of the proppants is seen in
 460 terms of proppant bed.
 461

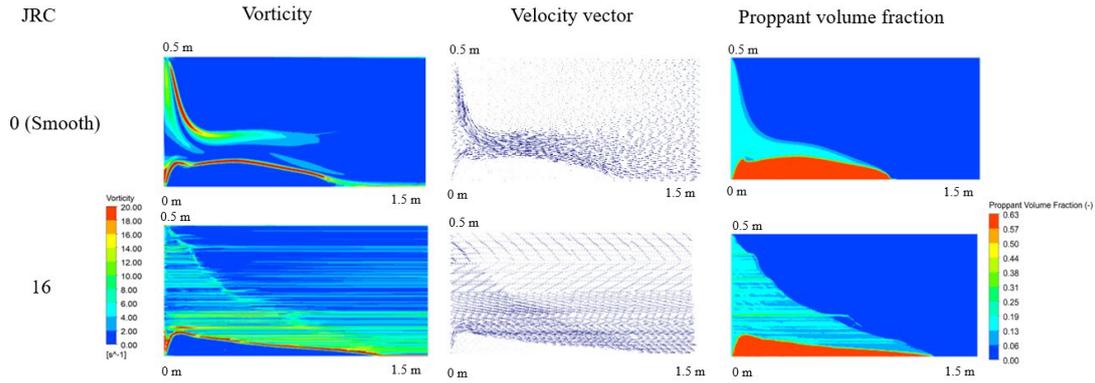
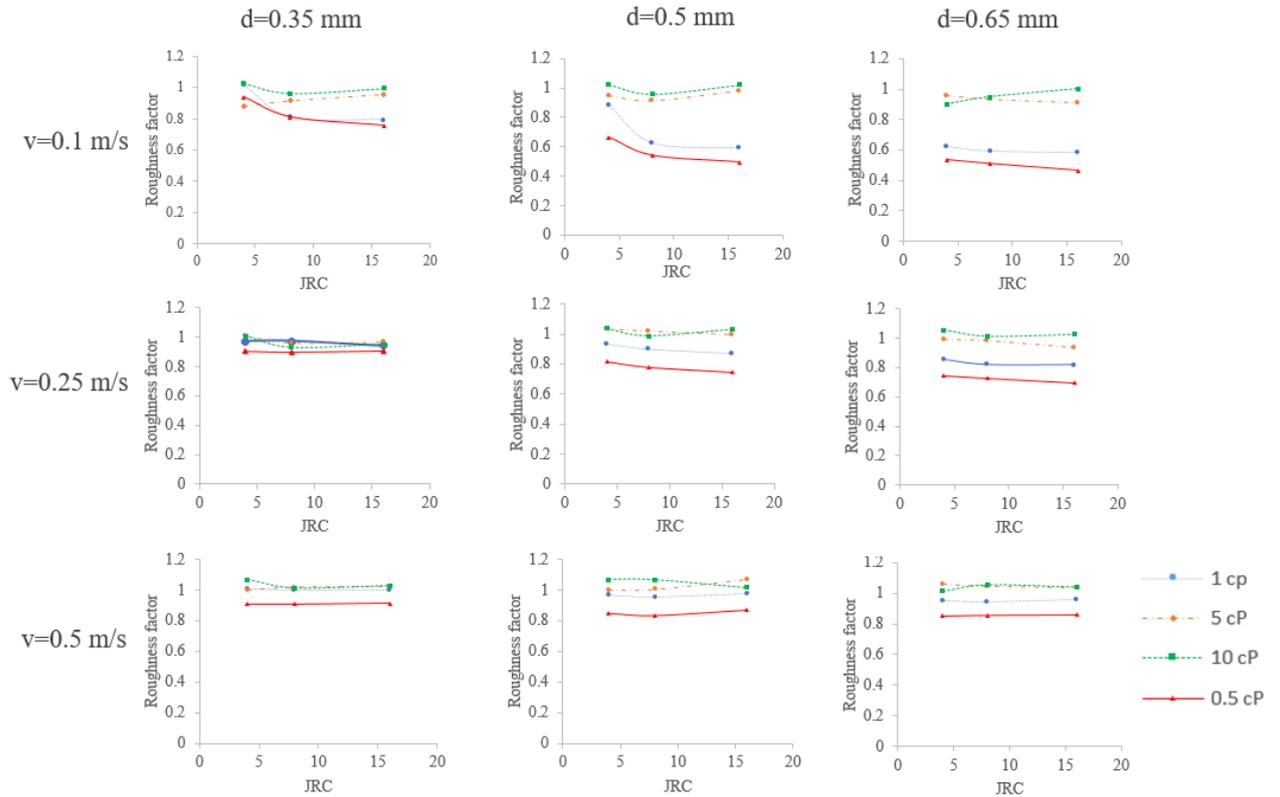


Fig. 14. Comparison of proppant transport in smooth fracture and rough fracture with JRC 16

As analysed above, the fracture roughness plays a significant role in the hydrodynamics of proppant transport, and qualitative comparison of vorticity, longitudinal velocity and volume fraction is shown in Fig. 11-14. Next, to quantitatively investigate the effect of fracture roughness on the proppant transport and distribution, a fracture roughness factor is introduced which is defined as $\epsilon_R = (v_s/v_r)$. The fracture roughness factor is the ratio of proppant axial velocity in a smooth fracture (v_s) to that in the rough fracture (v_r). A detailed analysis was carried out to investigate the impact of JRC on proppant transport. Different proppant transport simulations were run using the hybrid CFD model explained earlier with varying proppant properties (proppant diameter), flow properties (injection rate and fluid viscosity) and geomechanical properties (fracture roughness JRC and fracture width) one at a time as summarised in Table 1.

Firstly, the effect of JRC fracture profiles on the roughness factor was analysed (Fig. 15). It can be interpreted from Fig. 15 that with the increase in JRC, the roughness factor decreases. This is particularly true under the influence of low injection velocities and higher diameter proppant size (Fig. 15(a-f)). This is due to the increase in fracture roughness results in an increase in the inter-proppant and proppant-fracture wall interactions. Thus, strong mechanical interactions cause more randomness in the flow and accelerate the proppants axial velocity, resulting in the roughness factor ϵ_R below 1. However, during the proppant transport in high viscosity fluid, the mechanical interaction-induced flow effects do not play a dominant role in proppant horizontal transport, which causes $\epsilon_R \approx 1$ and can be ignored, as shown in Fig. 15. Thus, the mechanical interaction-induced effects are strongly dependent on proppant transport regimes (injection velocity, proppant size and fluid viscosity).



489 **Fig. 15.** Variation of fracture roughness factor with JRC for different injection velocity, and
 490
 491 proppant size
 492

493 Because of the strong dependence of proppant transport in different flow regime, the transport
 494 regions should be defined. A dimensionless composite parameter is introduced (Ar/Re) which
 495 is a ratio of Archimedes number and Reynolds number. The Archimedes number denotes the
 496 ratio of buoyancy force to inertia force. Fig. 16 shows the plot between the fracture roughness
 497 factor ϵ_R and Ar/Re , which suggests that for a low value of Ar/Re , the fracture roughness factor
 498 varies mostly independent of Ar/Re . Conversely, when the ratio of $Ar/Re > 10$, the fracture
 499 roughness factor significantly decreases. This can be explained by when proppants are
 500 transported with high-viscous fracturing fluids; the proppant Reynolds number is small. This
 501 results in a relatively stable flow field inside the fracture and consequently, low mechanical
 502 interaction flow effects. However, when the proppants are transported with low-viscous fluids,
 503 the proppant Reynolds number is higher. This results in significantly higher inter-proppant and
 504 proppant-wall interactions and consequently increased mechanical interaction flow effects.
 505 Thus, proppant horizontal transport is greatly dependent on the fracture roughness and the ratio
 506 of Ar/Re .
 507

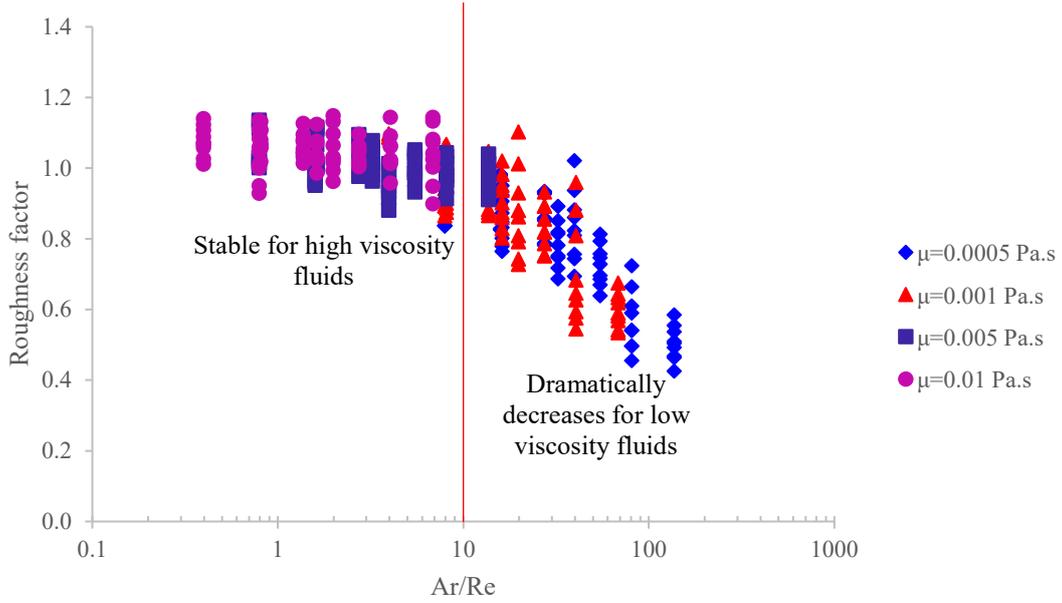


Fig. 16. Semi-log plot of fracture roughness factor with Ar/Re

508
509

510 Fig. 16 is categorised into two regions based on the variation of fracture roughness factor. In
511 the first region, the fracture roughness factor is almost constant and does not vary much against
512 Ar/Re for the range of Ar/Re between 0.3 and 10. The fracture roughness factor can be regarded
513 as primarily dependent on JRC, proppant size ratio and injection rate or velocity in this region,
514 and independent of the ratio of Ar/Re. Thus, a non-dimensional parameter $\Theta_{JRC} \left(\frac{d}{w} \right)$ is
515 proposed, and the plot of the roughness factor ϵ_R against the variation in the non-dimensional
516 parameter is shown in Fig. 17. Fig. 17 shows that fracture roughness factor varies linearly with
517 the change of non-dimensional parameter $\Theta_{JRC} \left(\frac{d}{w} \right)$ and Eq. 9 captures the variation of fracture
518 roughness factor against JRC and proppant size ratio for the range of Ar/Re between 0.3 and
519 10.

520

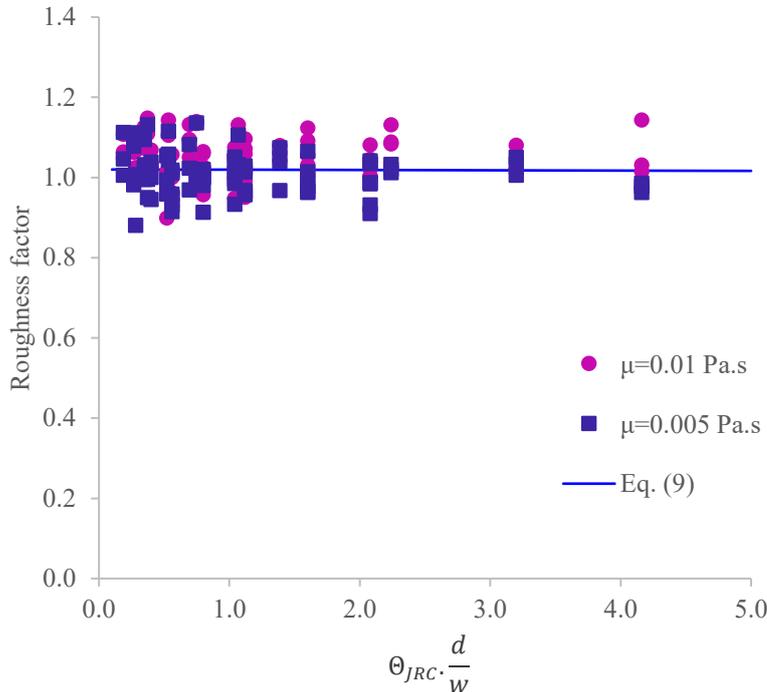
$$521 \quad \frac{V_s}{V_r} = 1 - 0.0007 * \Theta_{JRC} \frac{d}{w} \quad 0.3 \leq \frac{Ar}{Re} \leq 10 \quad (9)$$

522

523 From Fig. 16, the second region can be defined where the fracture roughness factor drastically
524 declines as $\frac{Ar}{Re}$ increases. This can be explained by when the proppant transport with low
525 viscosity fracturing fluids, the inter-proppant and proppant-wall interactions significantly
526 increases, resulting in higher mechanical interaction flow effects. The increase in fracture
527 roughness further adds to mechanical interactions and consequently, the mechanical interaction
528 flow effects become dominant and gradually governs the proppant transport. Thus, in this
529 region, the fracture roughness factor is dependent upon particle Reynolds number and
530 Archimedes number along with JRC, proppant size ratio and injection rate or velocity. A non-
531 dimensional variable that incorporates the effect of JRC, Ar/Re, and d/w is proposed,
532 $\frac{Re}{\Theta_{JRC} \cdot Ar} \left(\frac{w}{d} \right)$, and the plot of the roughness factor ϵ_R against the variation in the non-
533 dimensional parameter is shown in Fig. 18. Fig. 18(a) shows that with the increase of the
534 proposed non-dimensional parameter, due to the flow instabilities caused by the fracture
535 roughness and mechanical interaction flow effects, the fracture roughness factor efficaciously
536 increases initially and progressively stabilises to $\epsilon_R = 1$. To gain a better understanding of the
537 results at a lower value of non-dimensional parameter, the results are plotted on a semi-log
538 scale in Fig. 18(b). To encompass the effect of variation of fracture roughness factor on JRC,
539 Ar/Re, proppant size ratio and injection velocity, a new relationship is obtained and shown in
540 Eq. (10) that can aid the petroleum engineers to model the proppant transport in rough fractures.

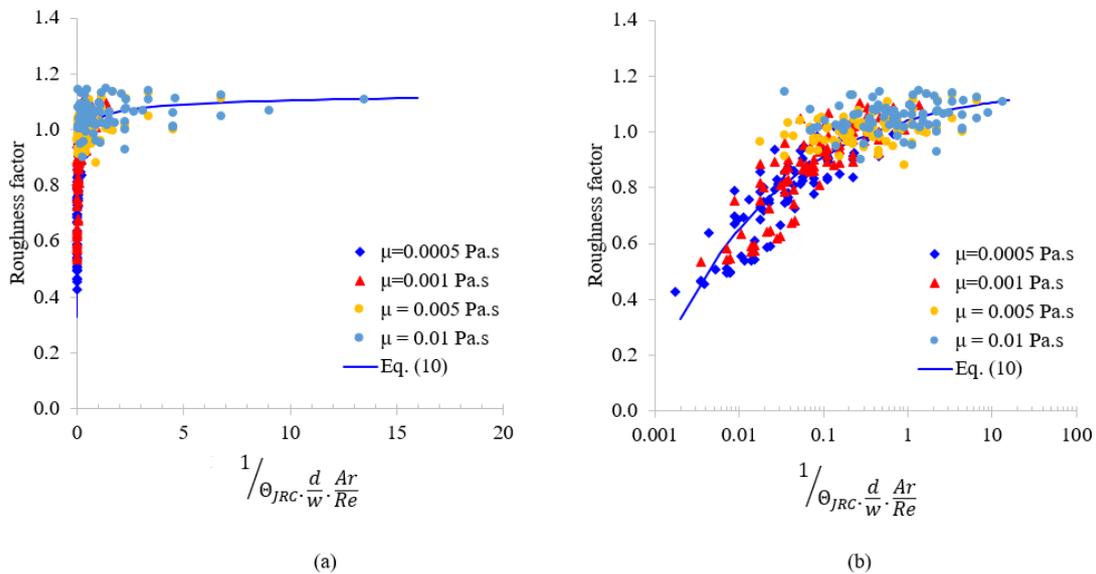
541
542

$$\frac{V_S}{V_R} = 1 - 0.13 * \left[\Theta_{JRC} \cdot \frac{d}{w} \cdot \frac{Ar}{Re} \right]^{0.3} \quad 11 \leq \frac{Ar}{Re} \leq 120 \quad (10)$$



543
544
545

Fig. 17. Variation of fracture roughness factor with JRC and proppant size ratio for $Ar/Re < 10$



546
547
548
549

Fig. 18. Variation of fracture roughness factor with JRC, proppant size ratio and Ar/Re for $Ar/Re > 10$

550 The correlation developed in the current study from Eq. (9) and Eq. (10) relates to the proppant
551 horizontal transport velocity against the fracture roughness (JRC), flow regime (Ar/Re), fluid
552 leak-off effects and proppant size ratio (d/w) in 3D fractures. A common assumption widely
553 used during the hydraulic fracturing simulation in shale gas reservoirs and modelling of
554 proppant transport is that the average proppant transport velocity is equal to the carrier
555 fracturing fluid velocity, and the proppant settling velocity follows Stokes' law (Blyton et al.,
556 2018). However, to accurately model the proppant transport and distribution, the effects of
557 fracture roughness, fluid leak-off, drag forces, gravity forces, inter-proppant and proppant-

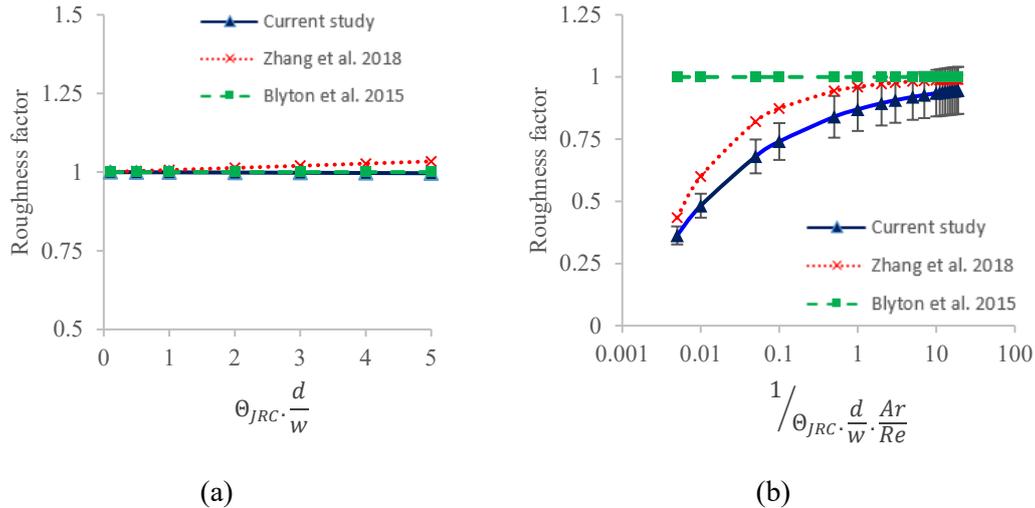
558 fracture wall interactions are required to be incorporated which is not included together in
 559 previous assumptions. The proposed correlation was compared against the existing studies,
 560 namely Zhang et al. (2019b) and Blyton et al. (2015). Zhang et al. (2019b) investigated the JRC
 561 fracture profiles and proposed a proppant transport model in rough fractures. However, the
 562 model is limited to two-dimensional fracture geometry, and gravitational effects along with
 563 fluid-leak off effects were ignored. The correlation proposed by Zhang et al. (2019b) is shown
 564 in Eq. (11). On the other hand, Blyton et al. (2015) comprehensively investigated the proppant
 565 transport in hydraulic fractures using CFD-DEM method and proposed a correlation for
 566 proppant settling velocity against different proppant size ratio. However, the effect of fracture
 567 roughness was ignored in the proppant hydrodynamics. The correlation proposed by Blyton et
 568 al. (2015) is shown in Eq. (12).

$$569 \quad \frac{V_r}{V_s} = \begin{cases} 1 - 0.0066 \cdot \Theta_{JRC} \frac{d}{w} \frac{v_i}{\sqrt{gd}} & 0.78 \leq \frac{Ar}{Re} \leq 11.15 \\ 1 - \frac{\Theta_{JRC} \frac{d}{w} \frac{v_i}{\sqrt{gd}}}{\Theta_{JRC} \frac{d}{w} \frac{v_i}{\sqrt{gd}} + 238.56 \frac{Re}{Ar}} & 11.15 \leq \frac{Ar}{Re} \leq 394.92 \end{cases} \quad (11)$$

$$570 \quad \frac{V_p}{V_f} = \begin{cases} 1 & \frac{d}{w} < 0.4 \\ -1.73 \left(\frac{d}{w}\right)^3 + 2.45 \left(\frac{d}{w}\right)^2 - 0.69 \left(\frac{d}{w}\right) + 1 & 0.4 < \frac{d}{w} < 0.95 \\ -21.45 \left(\frac{d}{w}\right) + 21.45 & \frac{d}{w} > 0.95 \end{cases} \quad (12)$$

571
 572 Fig. 19 shows a comparison of the correlation proposed in Eq. (9) and Eq. (10) in the current
 573 study with the previous studies of Zhang et al. (2019b) and Blyton et al. (2015). Fig. 19(a)
 574 shows the effect of fracture roughness on proppant transport under the influence of high
 575 viscosity fracturing fluid. As discussed earlier, when the proppants are transported with high-
 576 viscous fracturing fluids; the proppant Reynolds number is small. This results in a relatively
 577 stable flow field inside the fracture and consequently, low mechanical interaction flow effects.
 578 Thus, under the influence of high viscosity fracturing fluid, no significant variation in terms of
 579 roughness factor is noticed on comparison of the proposed correlation with the study of Zhang
 580 et al. (2019b) and Blyton et al. (2015). On the other hand, Fig. 19(b) shows the effect of fracture
 581 roughness on proppant transport under the influence of low viscosity fracturing fluid like slick
 582 water, which is commonly used in hydraulic fracturing of shale gas reservoirs. When the
 583 proppants are transported with low-viscous fluids, the proppant Reynolds number is higher.
 584 This results in significantly higher inter-proppant and proppant-wall interactions and
 585 consequently increased mechanical interaction flow effects. Thus, on comparison of the
 586 proposed correlation in the current study with the study of Zhang et al. (2019b) and Blyton et
 587 al. (2015) shows that since Blyton et al. (2015) ignored the effect of fracture roughness, the
 588 turbulence and mechanical interaction flow effects caused due to the increased proppant-
 589 fracture rough wall interactions were missed in the proppant transport prediction. The proppant
 590 transport model proposed by Zhang et al. (2019b) on the other hand, although included the
 591 effects of fracture roughness and is able to capture the mechanical interaction flow effects, but
 592 is limited to two-dimensional fracture geometry with no gravitational and fluid leak-off effects.
 593 On comparison of the current model with the results proposed by Zhang et al. (2019b) in Fig.
 594 19(b) suggests that the results from Zhang et al. (2019b) underpredict by approximately 20%
 595 the proppant transport and distribution due to the assumption of no fluid-leak off, no
 596 gravitational effects, and two-dimensional fracture geometry which significantly affects the
 597 inter-proppant and proppant-fracture wall interactions. Thus, the applicability of the proposed
 598 proppant transport model with fluid leakage and fracture roughness can help petroleum
 599 engineers to design the hydraulic fracturing operation with fewer limiting assumptions
 600 successfully.

601
 602



603 **Fig. 19.** Comparison of the proposed correlation with the previous studies (a) for high
604 viscosity fracturing fluid (b) for low viscosity fracturing fluid

605
606 The proppant transport in the current study accounts for the effect of fracture roughness, fluid
607 leak-off from the fracture walls, inter-proppant and proppant-fracture wall interactions. As
608 mentioned previously, no dynamic fracture propagation and fracture mechanics is considered
609 in the current model. The current proppant transport model can further be coupled with the
610 dynamic fracture propagation and upscaled to the industrial fractures. However, the proppant
611 transport model developed accounting the integrated effects of fracture roughness, fluid leak-
612 off, inter-proppant and proppant-fracture wall interactions can be incorporated into a complete
613 3D hydraulic fracture simulation study of shale gas reservoirs. The 3D complete hydraulic
614 fracturing simulation study in shale gas reservoirs will couple the fracture geomechanics, fluid
615 flow and proppant transport in hydraulic fractures to more accurately determine the pressure
616 drop, fluid flow and production efficiency in shale gas reservoirs (Zhang and Sun, 2019). A
617 dynamic and integrated numerical model that uses CFD technique to model the fluid flow with
618 proppant transport and Extended finite element method (XFEM) to model the fracture
619 propagation is discussed in detail in our recent work (Suri et al., 2020b).

620
621 In order to investigate the applicability of the current proppant transport model with the real
622 fractures, the current model was compared with the field observations from the hydraulic
623 fracturing in shale gas reservoir. Raterman et al. (2018) investigated the hydraulic fracture
624 propagation from the coring results extracted from a pilot well offset from an adjacent
625 hydraulically fractured well. It was reported that although the stimulated hydraulic fractures
626 were more than 1,000 ft (305 m), the proppant transport distribution was inefficient and limited
627 to merely 75 ft (23 m) from the wellbore. Secondly, Kurison et al. (2019a) validated long
628 hydraulic fractures in a carbonate-rich ultra-low permeability reservoir using fracture modelling
629 and observations from chemical tracers, microseismic, pressure interference and reservoir
630 simulation. Furthermore, Kurison et al. (2019b) used data analytics approach to correlate well
631 production performance with hydraulic fracturing stimulation parameters for wells in Eagle
632 Ford and Utica shale reservoirs. Thus, the hydraulic fracture geometry was derived from the
633 Kurison et al. (2019a) study of fracture half-length 800 ft (245 m) and fracture height of 125 ft
634 (38 m) to investigate the proppant transport. The fracture width was assumed as 10 mm. Kurison
635 et al. (2019b) provided estimates of average volumes of hydraulic fracturing cluster stimulation
636 for two shale plays. The typical field average for hydraulic fracturing fluid volumes for single
637 perforation clusters in a single wing of the bi-wing fracture is approximately 1500 bbls
638 (equivalent to 3000 bbls fluid volume for a bi-wing fracture). The typical injection time is 60
639 min, which translates to the fluid flow rate of 36,000 bbl/d (0.06625 m³/s). The proppants
640 injected per cluster estimated by Kurison et al (2019b) is 50,000 lbs for a single wing fracture

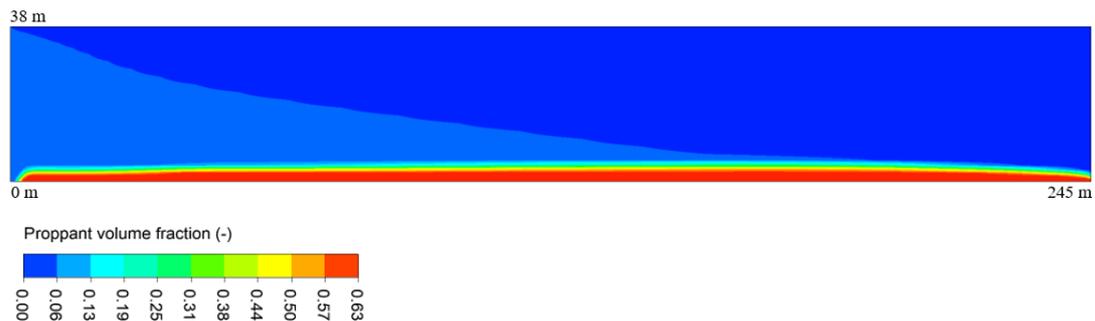
641 (equivalent to 100,000 lbs for a bi-wing fracture). This translates to the proppant concentration
 642 of 0.794 lbs/gal. Thus, using this proppant concentration and typical proppant density of 2650
 643 kg/m³, the proppant volume fraction calculated and used in the model is 3.6%. The key physical
 644 properties used in the simulation are detailed in Table 2 which are based on the study of
 645 Raterman et al. (2018) and Kurison et al. (2019b). The current hybrid proppant transport model
 646 with an assumed JRC of 4 based on the fracture and core images from Raterman et al. (2018)
 647 was used in the simulation. The injection time used is 60 min. Fig. 20 shows the result of
 648 proppant distribution after 60 min of injection. The proppant volume fraction plot in Fig. 20
 649 shows that the proppant deposits at the fracture bottom and forms a proppant bed. For the
 650 injection time of 60 min, the proppant laterally extends to the entire length of the hydraulic
 651 fracture of 245 m. However, in terms of proppant bed height, the average proppant bed height
 652 formed after 60 min of injection is approximately 5.5 m. It is to be noted that once the injection
 653 of fracturing fluid stops, the unpropped section of the hydraulic fracture closes down due to the
 654 surrounding geomechanical stresses and reservoir pressure. The fracture closure post-injection
 655 is not modelled as it is out of the scope of the current study. Additionally, the average proppant
 656 horizontal transport velocity is calculated from the numerical simulation at 35 m from the inlet
 657 and compared with the velocity predicted from the Eq. (9) based on the ratio of Ar/Re. The
 658 average proppant horizontal transport velocity from the numerical simulation is 0.21 m/s and
 659 from the Eq. (9) is 0.205 m/s, which shows a good agreement and applicability of the current
 660 model in simulating the real fractures.

661
 662
 663

Table 2
 Key physical parameters used in the simulation

Property	Value
Fracture dimension	245 m × 38 m × 0.01 m
Injection rate	0.06625 m ³ /s (3600 bbl/d)
Proppant size	0.284 mm (40/70 size sand)
Proppant concentration	0.794 lbs/gal
Proppant density	2650 kg/m ³
Proppant volume fraction	0.036
Slick water density	1000 kg/m ³
Assumed fluid viscosity	0.001 Pa.s
JRC	4

664



665
 666

Fig. 20. Proppant transport in industrial-scale hydraulic fracture

667
 668
 669
 670
 671
 672
 673
 674
 675

The proppant transport and distribution in a hydraulic fracture depends on a combination of multiple physical parameters. A detailed discussion of the parametric study about the role of proppant size, injection rate, fluid viscosity and proppant concentration in improving the proppant distribution can be found in our recent work (Suri et al., 2020a, 2020b). In order to improve the proppant transport efficiency firstly, the proppant injection time has to be sufficient enough so that the proppant can successfully distribute to the maximum stimulated hydraulic fracture volume. This can be achieved by correctly modelling the proppant transport physics as detailed in the current model. Secondly, the improvement in the proppant transport sweep

676 efficiency in the fracture can be achieved by varying the injection rates or using intermittent
677 injection cycle. This is explained in detail in Suri et al. (2020b) where it was observed that using
678 the multiple cycles of proppant injection followed by flushing pad fluid improved the proppant
679 transport sweep efficiency. Thirdly, another important parameter that significantly improves
680 the proppant transport and distribution is injecting proppants with varying size. Suri et al.
681 (2020a) explained that one of the effective approaches for improving the proppant transport
682 efficiency in the fracture is injecting the fracturing fluid slurry with smaller size proppants
683 followed by larger size proppant particles. This is particularly true for the low viscosity
684 fracturing fluid such as slick water which is commonly used in hydraulic fracturing of shale
685 reservoirs. The smaller size proppants possess a greater suspension ability in the fracturing
686 fluid, and thus injecting the proppant with variation in size results in improved proppant sweep
687 efficiency and can lead to more uniform fracture conductivity (Suri et al., 2020a). Lastly, the
688 fracturing fluid viscosity plays an important role in improving the efficiency of proppant
689 transport (Suri et al., 2020a, 2020b). Suri et al. (2020b) explained that the low viscosity
690 fracturing fluid such as slick water, due to its poor ability for proppant suspension results in a
691 quick deposition of the proppants after injection. This could eventually form a proppant bridge
692 and fracture tip screen-out depending upon the fracture height, which could further lead to a
693 substantial area of fracture remaining unpropped and closing down when the hydraulic pressure
694 is removed. On the contrary, the higher viscosity fracturing fluid due to its better proppant
695 suspension ability can suspend the proppants for a longer period and thus resulting in more
696 extended proppant transport inside the fracture (Suri et al., 2020b). Thus, it can be summarised
697 from the above discussion that the proppant transport efficiency in the hydraulic fracture can
698 be improved using an appropriate combination of injection rate, proppant size, injection time,
699 and fracturing fluid viscosity. The current proppant transport model described in this study can
700 be used to successfully simulate the proppant transport physics by varying different parameters
701 and can aid the petroleum engineers to improve the hydraulic fracturing design.

702 703 **4. Conclusions**

704
705 Proppant transport and distribution is studied in the rough hydraulic fractures using the Hybrid
706 method (CFD-DEM). The effect of fracture Joint Roughness Coefficient (JRC) was
707 quantitatively investigated on proppant motion. For the fluid flow and proppant transport in
708 smooth fractures, the fracture walls employ substantial mechanical retardation effects on
709 proppants resulting in a decrease of proppant horizontal transport velocity and greater proppant
710 deposition. In contrast, when the proppants are transported in rough fractures, with the increase
711 in fracture roughness the inter proppant and proppant -wall interactions dramatically increase,
712 and consequently higher amount of proppant is suspended in the slurry resulting in greater
713 proppant horizontal transport velocity. Furthermore, in terms of horizontal motion, proppants
714 are inclined to transport a long distance away from the wellbore with the increase in fracture
715 roughness. The mechanical interaction flow effects were found to be dependent on the proppant
716 transport regime. When the proppant transport in high viscosity fluids (i.e. at low proppant
717 Reynolds number), no significant effect of fracture roughness in proppant transport is noticed.
718 In contrast, for proppant transport in low viscosity fluids (i.e. at high proppant Reynolds
719 number), the mechanical interaction effects become dominant with roughness and significantly
720 increases proppant horizontal transport velocity.

721 722 **Acknowledgement**

723 The authors are grateful to the School of Engineering, Robert Gordon University, Aberdeen,
724 United Kingdom, for supporting this research.

725 726 **Conflicts of Interest**

727 The authors declare no conflicts of interest.
728
729
730

731 **References**

732
733
734
735
736
737
738
739
740
741
742
743
744
745
746
747
748
749
750
751
752
753
754
755
756
757
758
759
760
761
762
763
764
765
766
767
768
769
770
771
772
773
774
775
776
777
778
779
780
781
782
783
784

Alves, L.M., 2012. Foundations of measurement fractal theory for the fracture mechanics, in: Belov, A. (Ed.), Applied Fracture Mechanics. Intech, Bari, pp. 19-66. <http://dx.doi.org/10.5772/51813>.

Arsenijević, Z.L., Grbavčić, Ž, Garić-Grulović, R., Bošković-Vragolović, N., 2010. Wall effects on the velocities of a single sphere settling in a stagnant and counter-current fluid and rising in a co-current fluid. Powder Technol. 203, 237-242. <https://doi.org/10.1016/j.powtec.2010.05.013>.

Barton, N., Choubey, V., 1977. The shear strength of rock joints in theory and practice. Rock Mech. 10, 1-54. <https://doi.org/10.1007/BF01261801>.

Blyton, C.A., Gala, D.P., Sharma, M.M., 2015. A comprehensive study of proppant transport in a hydraulic fracture. In: Paper SPE-174973-MS, SPE Annual Technical Conference and Exhibition, 28-30 September, Houston, Texas, USA. Society of Petroleum Engineers. <https://doi.org/10.2118/174973-MS>.

Blyton, C.A., Gala, D.P., Sharma, M.M., 2018. A Study of Proppant Transport with Fluid Flow in a Hydraulic Fracture. SPE Drill Completion. 33, 307-323. <https://doi.org/10.2118/174973-PA>.

Bokane, A.B., Jain, S., Crespo, F., 2014. Evaluation and Optimization of Proppant Distribution in Multistage Fractured Horizontal Wells: A Simulation Approach. In: Paper SPE-171581-MS, SPE/CSUR Unconventional Resources Conference – Canada, 30 September–2 October, Calgary, Alberta, Canada. Society of Petroleum Engineers. <https://doi.org/10.2118/171581-MS>.

Briggs, S., Karney, B.W., Sleep, B.E., 2017. Numerical modeling of the effects of roughness on flow and eddy formation in fractures. J. Rock Mech. Geotec. Eng. 9, 105-115. <https://doi.org/10.1016/j.jrmge.2016.08.004>.

Chalov, S.R., Jarsjö, J., Kasimov, N.S., Romanchenko, A.O., Pietróń, J., Thorslund, J., Promakhova, E.V., 2015. Spatio-temporal variation of sediment transport in the Selenga River Basin, Mongolia and Russia. Environ. Earth Sci. 73, 663-680. <https://doi.org/10.1007/s12665-014-3106-z>.

Chhabra, R., Agarwal, S., Chaudhary, K., 2003. A note on wall effect on the terminal falling velocity of a sphere in quiescent Newtonian media in cylindrical tubes. Powder Technol. 129, 53-58. [https://doi.org/10.1016/S0032-5910\(02\)00164-X](https://doi.org/10.1016/S0032-5910(02)00164-X).

Delidis, P., Stamatoudis, M., 2009. Comparison of the velocities and the wall effect between spheres and cubes in the accelerating region. Chem. Eng. Commun. 196, 841-853. <https://doi.org/10.1080/00986440802668182>.

Deshpande, Y.K., Crespo, F., Bokane, A.B., Jain, S., 2013. Computational fluid dynamics (CFD) study and investigation of proppant transport and distribution in multistage fractured horizontal wells. In: Paper SPE-165952-MS, SPE Reservoir Characterization and Simulation Conference and Exhibition, 16-18 September, Abu Dhabi, UAE. Society of Petroleum Engineers. <https://doi.org/10.2118/165952-MS>.

Dontsov, E.V., Peirce, A.P., 2014. Slurry flow, gravitational settling and a proppant transport model for hydraulic fractures. J. Fluid Mech. 760, 567-590. <https://doi.org/10.1017/jfm.2014.606>.

Hu, X., Wu, K., Li, G., Tang, J., Shen, Z., 2018. Effect of proppant addition schedule on the proppant distribution in a straight fracture for slickwater treatment. J. Pet. Sci. Eng. 167, 110-119. <https://doi.org/10.1016/j.petrol.2018.03.081>.

Kassis, S., Sondergeld, C.H., 2010. Fracture permeability of gas shale: Effect of roughness, fracture offset, proppant, and effective stress. In: Paper SPE-131376-MS, International oil and gas conference and exhibition, 8-10 June, Beijing, China. Society of Petroleum Engineers. <https://doi.org/10.2118/131376-MS>.

Kou, R., Moridis, G.J., Blasingame, T., 2018. Field Scale Proppant Transport Simulation and Its Application to Optimize Stimulation Strategy. In: Paper URTEC-2878230-MS, SPE/AAPG/SEG Unconventional Resources Technology Conference, 23-25 July

785 2018, Houston, Texas, USA. Society of Petroleum Engineers.
786 <https://doi.org/10.15530/urtec-2018-2878230>.

787 Kurison, C., Kuleli, H.S., Mubarak, A.H., Al-Sultan, A., Shehri, S.J., 2019a. Reducing
788 uncertainty in unconventional reservoir hydraulic fracture modeling: A case study in
789 Saudi Arabia. *J. Nat. Gas Sci. Eng.* 71, 102948.
790 <https://doi.org/10.1016/j.jngse.2019.102948>.

791 Kurison, C., Kuleli, H.S., Mubarak, A.H., 2019b. Unlocking well productivity drivers in Eagle
792 Ford and Utica unconventional resources through data analytics. *J. Nat. Gas Sci. Eng.*
793 71, 102976. <https://doi.org/10.1016/j.jngse.2019.102976>

794 Li, P., Zhang, X., Lu, X., 2018. Numerical simulation on solid-liquid two-phase flow in cross
795 fractures. *Chem. Eng. Sci.* 181, 1-18. <https://doi.org/10.1016/j.ces.2018.02.001>.

796 Malhotra, S., Sharma, M.M., 2012. Settling of spherical particles in unbounded and confined
797 surfactant-based shear thinning viscoelastic fluids: An experimental study. *Chem. Eng.*
798 *Sci.* 84, 646-655. <https://doi.org/10.1016/j.ces.2012.09.010>.

799 Mandelbrot, B.B., 1983. *The fractal geometry of nature*. WH freeman, New York.

800 Ogilvie, S.R., Isakov, E., Glover, P.W., 2006. Fluid flow through rough fractures in rocks. II:
801 A new matching model for rough rock fractures. *Earth Planet. Sci. Lett.* 241, 454-465.
802 <https://doi.org/10.1016/j.epsl.2005.11.041>.

803 Patankar, N.A., Joseph, D.D., 2001. Modeling and numerical simulation of particulate flows by
804 the Eulerian–Lagrangian approach. *Int. J. Multiph. Flow.* 27, 1659-1684.
805 [https://doi.org/10.1016/S0301-9322\(01\)00021-0](https://doi.org/10.1016/S0301-9322(01)00021-0).

806 Raterman, K.T., Farrell, H.E., Mora, O.S., Janssen, A.L., Gomez, G.A., Busetti, S., McEwen,
807 J., Frieauf, K., Rutherford, J., Reid, R., 2018. Sampling a Stimulated Rock Volume: An
808 Eagle Ford Example. *SPE Reserv. Evaluation Eng.* 21, 927-941.
809 <https://doi.org/10.2118/191375-PA>.

810 Sahai, R., Miskimins, J.L., Olson, K.E., 2014. Laboratory results of proppant transport in
811 complex fracture systems. In: Paper SPE-168579-MS, SPE Hydraulic Fracturing
812 Technology Conference, 4-6 February, The Woodlands, Texas, USA. Society of
813 Petroleum Engineers. <https://doi.org/10.2118/168579-MS>.

814 Sahu, A., Tripathy, A., Biswal, S., 2013. Study on particle dynamics in different cross sectional
815 shapes of air dense medium fluidized bed separator. *Fuel.* 111, 472-477.
816 <https://doi.org/10.1016/j.fuel.2013.04.011>.

817 Smith, M.B., Montgomery, C., 2015. *Hydraulic fracturing*. CRC Press, Boca Raton, Florida.
818 <https://doi.org/10.1201/b16287>.

819 Speight, J.G., 2016. *Handbook of Hydraulic Fracturing*. John Wiley & Sons, Inc., Hoboken,
820 New Jersey. <https://doi.org/10.1002/9781119225102>.

821 Suri, Y., Islam, S.Z., Hossain, M., 2019. A new CFD approach for proppant transport in
822 unconventional hydraulic fractures. *J. Nat. Gas Sci. Eng.* 70, 102951.
823 <https://doi.org/10.1016/j.jngse.2019.102951>.

824 Suri, Y., Islam, S.Z., Hossain, M., 2020a. Numerical modelling of proppant transport in
825 hydraulic fractures. *Fluid Dyn. Mater. Process.* 16, 297-337.
826 <https://doi.org/10.32604/fdmp.2020.08421>.

827 Suri, Y., Islam, S.Z., Hossain, M., 2020b. Proppant transport in dynamically propagating
828 hydraulic fractures using CFD-XFEM approach. *Int. J. Rock Mech. Min. Sci.* 131,
829 104356. <https://doi.org/10.1016/j.ijrmms.2020.104356>.

830 Tan, Q., 2011. *Dimensional analysis: with case studies in mechanics*. Springer Science &
831 Business Media, Berlin. <https://doi.org/10.1007/978-3-642-19234-0>.

832 Tong, S., Mohanty, K.K., 2016. Proppant transport study in fractures with intersections. *Fuel.*
833 181, 463-477. <https://doi.org/10.1016/j.fuel.2016.04.144>.

834 Uddameri, V., Morse, A., Tindle, K.J., 2015. *Hydraulic fracturing impacts and technologies: A
835 multidisciplinary perspective*. CRC Press, Boca Raton, Florida.
836 <https://doi.org/10.1201/b18581>

837 Veatch, R.W., King, G.E., Holditch, S.A., 2017. *Essentials of hydraulic fracturing: Vertical and
838 horizontal wellbores*. PennWell Corporation, Tulsa, Oklahoma.

839 Zhang, G., Zhang, Y., Xu, A., Li, Y., 2019a. Microflow effects on the hydraulic aperture of
840 single rough fractures. *Adv. Geo-Energy Res.* 3, 104-114.
841 <https://doi.org/10.26804/ager.2019.01.09>.
842 Zhang, G., Gutierrez, M., Chao, K., 2019b. Hydrodynamic and mechanical behavior of multi-
843 particle confined between two parallel plates. *Adv. Powder Technol.* 30, 439-450.
844 <https://doi.org/10.1016/j.appt.2018.11.023>.
845 Zhang, G., Gutierrez, M., Li, M., 2017. A coupled CFD-DEM approach to model particle-fluid
846 mixture transport between two parallel plates to improve understanding of proppant
847 micromechanics in hydraulic fractures. *Powder Technol.* 308, 235-248.
848 <https://doi.org/10.1016/j.powtec.2016.11.055>.
849 Zhang, G., Li, M., Xue, J., Wang, L., Tian, J., 2016. Wall-retardation effects on particles settling
850 through non-Newtonian fluids in parallel plates. *Chem. Pap.* 70, 1389-1398.
851 <https://doi.org/10.1515/chempap-2016-0082>.
852 Zhang, J., Dunn-Norman, S., 2015. Computational fluid dynamics (CFD) modeling of proppant
853 transport in a plug and perf completion with different perforation phasing. In:
854 Paper URTEC-2169184-MS, Unconventional Resources Technology Conference, 20-22
855 July 2015, San Antonio, Texas, USA. Society of Petroleum Engineers.
856 <https://doi.org/10.15530/urtec-2015-2169184>.
857 Zhang, T., Sun, S., 2019. A coupled Lattice Boltzmann approach to simulate gas flow and
858 transport in shale reservoirs with dynamic sorption. *Fuel.* 246, 196-203.
859 <https://doi.org/10.1016/j.fuel.2019.02.117>.

860

861 **Nomenclature**

862	\vec{F}_{KTGF}	Inter-particle interaction force from kinetic theory of granular flow
863	\vec{M}_{Is}	Interfacial momentum transfer
864	ϵ_R	Fracture roughness factor
865	C_D	Drag coefficient
866	S_m	Mass source term
867	S_u	Momentum source term
868	\vec{v}	Velocity
869	τ_r	Particle relaxation time
870	Φ_b	Basic friction angle
871	V_{inj}	Injection velocity
872	c_L	Fluid leak-off rate constant
873	v_r	Velocity in rough fracture
874	v_s	Velocity in a smooth fracture
875	σ_c	Fracture compressive strength
876	σ_n	Effective normal stress
877	Ar	Archimedes number
878	CFD	Computational fluid dynamics
879	d	Proppant diameter (size)
880	DEM	Discrete element method
881	g	Acceleration due to gravity
882	JRC	Joint roughness coefficient
883	KTGF	Kinetic theory of granular flow
884	P	Pressure
885	Re	Reynolds number
886	t	Current time step
887	UDF	User-defined function
888	w	Fracture width

889	α	Volume fraction
890	μ	Dynamic viscosity
891	ρ	Density
892	τ	Maximum shear strength
893	θ_{JRC}	Joint roughness coefficient
894		
895	Subscripts:	
896	i	Phase (liquid or solid)
897	l	Liquid phase
898	p	Particle phase
899	s	Granular phase