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1

2 **A multi-criteria group decision-making method for the** 3 **thermal renovation of masonry buildings: the case of** 4 **Algeria**

5

6

7 **Abstract**

8 The future of masonry buildings with heritage values is certain – the investments in making such
9 buildings energy-efficient during renovations to meet the energy consumption requirements will
10 increase over the next decade. However, decision makers fail to address the concerns of each
11 project actor and give specific answers on how basic requirements on such historical buildings can
12 be implemented. This paper proposes a new multi-criteria group decision-making method for the
13 thermal renovation of masonry buildings. The aim of the proposed method is to rank different
14 renovation solutions. The method uses; the structured group interaction method Delphi to define
15 the evaluation criteria and the thermal renovations solutions, Swing method to facilitate the process
16 of the determination of the criteria weights, the group decision support system (PROMETHEE
17 GDSS) to reach a global ranking of the renovations solutions, PROMETHEEV to introduce
18 additional constraints, as well as the Graphical Analysis for Interactive Aid (GAIA) analysis to get
19 a better understanding of conflicts and similarities between the criteria and among the decision
20 makers. We proceed to exemplify by means of a real-life case project in Algeria and offer
21 suggestions on what front-ended stakeholders could do to reduce the energy consumption in
22 masonry buildings.

23 Keywords: thermal renovation, masonry buildings, PROMETHEE methods, multi-criteria
24 decision-making, group decision.

25 **1 Introduction**

26 Residential and tertiary sectors in Algeria consume about 34%of the total energy production in the
27 country. The government has launched in 2016 a thermal renovation program for existing buildings
28 to reduce the energy consumption. This program is led by the national agency for the promotion
29 and the rationalization of the energy use (APRUE). It aims to insulate 100.000 houses per year.
30 The national fund for energy management (FNME) will provide 80percent of the costs related to
31 these interventions [1].The existing building stock in Algeria has reached 6,500,000dwellings in
32 2016, from those 1,050,000 consist of masonry dwellings built before 1945. The majority of
33 masonry buildings were built during the French colonial period. These buildings rep-resent a
34 valuable architectural heritage. They were constructed using traditional techniques and materials
35 (for e.g. load bearing walls of stone masonry, vaulted brick floor and metal beams) [2].The masonry
36 buildings are subject in Algeria to a wide preservation program, many buildings rehabilitations are
37 undertaken across the country. In 2016, the government envisages the diagnostics of 300.000
38 dwellings. Rehabilitation operations will be launched following these diagnostics. These actions
39 will be conducted and financed by the government. The buildings rehabilitation will concern only
40 common parts of buildings (exterior facades, yards, cellars, entrance halls, stairwells, accessible
41 and inaccessible terraces, and pitched roofs) [3].The energy-saving program in the residential
42 sector and the rehabilitation of masonry buildings program offer a great opportunity to perform the
43 thermal renovation of masonry buildings. This will balance between the improvement of the
44 thermal performance of the existing buildings stock and the perseveration of masonry buildings.
45 However, the choice of improvement alternatives during their thermal renovation is a complex
46 decision because:

- 47 • It involves different stakeholders (actor concerned with the preservation of buildings, actor
48 concerned by the reduction of energy consumption, building users, and so on) that can
49 express a multitude of criteria (economic, energy, cultural, historical, and so on).
- 50 • The communication among the actors to obtain a consensus regarding the definition of
51 evaluation criteria, and the potential thermal renovation solutions might be complicated due
52 the differences in their respective backgrounds.
- 53 • The difficulty in assessing the importance of each criterion for each actor.

54 Due to the multi-decision makers and multi-criteria character of the thermal renovation of masonry
55 buildings in Algeria, it is difficult to find solutions that can optimize all the criteria at once.
56 Therefore, it would be more appropriate to find consensus solutions. The multiple-criteria decision
57 analysis is a useful tool for this type of problem; it evaluates different solutions taking into account
58 both the preferences of decision makers and the different criteria. Many research studied the
59 application of multi-criteria decision methods in the renovation of masonry buildings [4–7]. Yet,
60 only few works focused on the use of such methods in order to make masonry buildings energy-
61 efficient [8–10]. This paper pro-poses a new group decision aid method that combines the Delphi
62 method, the Swing method, and the Preference Ranking Organization Method for Enrichment
63 Evaluation PROMETHEE methods [11] for the thermal renovation of masonry buildings with a
64 heritage value. The aim of the proposed method is to rank different thermal renovation solutions
65 using a multi-criteria and multi-decision makers approach. This paper is divided into six-parts, the
66 following section presents a literature review concerning the application of multi-criteria decision
67 aid methods in the field of thermal renovation, part 3 develops the method used in this paper, part
68 4 provides the results of the application of the method on a case study, Section 5 evaluates the
69 proposed method, while Section 6 presents conclusions and directions for future research.

71 **2 Literature review**

72 Different methods were applied to support decisions for the thermal renovation of buildings [8–
73 10,12,13–26]. These methodologies can be categorized into two main families as indicated in
74 Zavadskas et al. [12]: the Multi-Criteria Decision Aid methods (MCDA), in which the numbers of
75 alternatives to consider is finite and known, and the Multi-Objective Optimization methods
76 (MOO), which enables the consideration of an infinite set of alternatives.

77 **2.1 Multi-criteria decision aid (MCDA) methods**

78 MCDA used for the thermal renovation of buildings can be ranked into two different approaches,
79 the partial aggregation approach, and the complete aggregations approach.

80 **2.1.1 The partial aggregation approaches**

81 The advantage of this approach is that it provides the opportunity to take into account both
82 quantitative and qualitative criteria without having to do any coding. It does not allow
83 compensation between criteria such as facing two actions “*a*” and “*b*” it is based on the assumption
84 that “*a*” outrank “*b*”, if “*a*” is at least as good as “*b*” on a majority of criteria without being too
85 much worse in other criteria. Rey [13] proposed an outranking MCDA with partial aggregation
86 from the ELECTRE (ELimination and Choice Expressing the REality) methods for the thermal
87 renovation of office buildings. Outranking methods were also applied to study air conditioning
88 systems [14]. Catalina et al. [15] applied MCDA method ELECTRE in order to select an
89 appropriate multi-source energy system for residential houses. Avgelis and Papadopoulos [16] used
90 ELECTRE in order to rank different HVAC systems in a university building regarding energy costs
91 and inflation, as well as the economic and life cycle costs of acquiring a system.

92 **2.1.2 The complete aggregation approach**

93 The complete aggregation approach gives a note to all scenarios, whilst basing the score on the
94 most important criteria. However, this approach presents several limitations. It allows the
95 compensation of low score in criteria with good results on several other criteria. Also, it is

96 necessary to carry out a coding while taking into account both quantitative and qualitative criteria.
97 Roulet et al. [17] suggested a multi-criteria rating methodology based on a complete aggregation
98 approach in order to assess the effectiveness of various thermal renovation scenarios.

99 Blondeau et al. [18] tested MAUT (Multi-Attribute Utility Theory) technic in the study of summer
100 ventilation strategies in an educational building. Their findings highlighted the limitations of this
101 method. It is completely compensatory and it sometimes provides counter-intuitive results. Alanne
102 [19] applied a multi-criteria decision aid model type “knapsack” to help designers to choose the
103 most appropriate renovation actions during the design phase of a project. The advantage of this
104 model is to treat a portfolio optimization case by introducing constraints. The disadvantage is the
105 purely additive character of the model.

106 Medineckiene and Björk [20] applied the multi-criteria decision aid method SAW (Simple Additive
107 Weighting), MEW (Multiplicative Exponential Weighting), and COPRAS (COMplex PROportion
108 ASsessment) to choose solutions for the thermal renovation of Swedish residential apartments.

109 Kontu et al. [21] proposed the multi-criteria decision aid method SMAA (Stochastic Multicriteria
110 Acceptability Analysis) to assess which heating system would be best for new single-family homes.
111 The advantage of both approaches cited in this paragraph is to take into account the preferences of
112 the building users, they were involved in the decision process using interviews for the first method
113 and questionnaire for the second in order to get their preferences regarding different evaluations
114 criteria.

115 Šiožinytė et al. [22] applied the TOPSIS Grey (Technique for Order Preference by Similarity to
116 Ideal Solution with grey numbers) and AHP (Analytic Hierarchy Process) methods to find the best
117 compromise solution in order to make vernacular buildings energy efficient. Different criteria were
118 considered, such as architectural heritage, requirements (norms), energy and comfort. Ruzgys et
119 al. [23] applied an integrated SWARA (Step-wise Weight Assessment Ratio Analysis) –TODIM
120 (an acronym in Portuguese of Interactive and Multi-criteria decision-making) multi-criteria

121 decision-making method in order to rank the best alternatives of residential building modernization
122 in Lithuania.

123 Terracciano et al. [9] have studied the analysis of vertical addition systems for energetic retrofitting
124 of existing masonry buildings. The multicriteria decision-making TOPSIS method have been used
125 in order to compare the vertical addition systems with each other in terms of structural,
126 environmental and economic performance parameters. Zagorskis et al. [10] applied TOPSIS
127 (Technique for Order of Preference by Similarity to Ideal Solution) method to select the best
128 insulation option for historic buildings among five internal insulation materials. This method takes
129 into account five criteria: cost of the material, complexity of the installation, heat transfer
130 coefficient, loss of space, and moisture properties of the material. The relevance of both methods
131 presented by Terracciano et al. [9], and Zagorskis et al. [10] compared to all the other methods
132 cited previously, is that they take into account the specificity of the thermal renovation of masonry
133 buildings with a heritage value. However, they both have several limitations, such as the method
134 proposed by Zagorskis et al. [10] can be applied only for the internal insulation of buildings, while
135 the method suggested by Terracciano et al. [9] can be used only for the selection of vertical addition
136 systems. In addition, both methods do not take into account the preferences of different decision
137 makers, and they are completely compensatory.

138 **2.2 Multi objective optimization (MOO) methods**

139 All the previous MCDA methods cited in subsection 2.1 assume that the number of action to
140 evaluate is finite. Multi objective optimization methods are relevant as they enable the user to
141 consider an infinite set of alternatives. Diakaki et al. [24] applied an MOO method to improve
142 energy efficiency in buildings. It allows considering an infinite number of actions and evaluating
143 them through various criteria. The evaluation criteria include the annual primary energy
144 consumption of the building, annual emissions of carbon dioxide and the initial cost investment.
145 Asadi et al. [25] proposed an MOO method to help stakeholders in the definition of intervention

146 measures. The method aims to minimize the use of energy in the building profitably while
147 satisfying the needs of the occupant. Asadi et al. [26] suggested an MOO method using genetic
148 algorithm capable of evaluating different scenarios in a renovation project. Different criteria were
149 considered including the energy consumption, the cost of the renovation, and the comfort of the
150 occupant. Brauers et al. [8] have presented the application of the MOO method MOORA (Multi-
151 Objective Optimisation by Ratio analysis) and MULTIMOORA (MOORA plus Full Multiplicative
152 Form) with discrete dimensionless measures in order to find an optimal solutions for the thermal
153 renovation of masonry buildings from the Soviet period.

154 Contrary to multi-criteria decision aid methods, Most of multi objective optimization methods do
155 not allow the ranking or the selection of the best solutions. They only allow the identification of a
156 set of effective solutions and the description of accessible compromises. Furthermore, the
157 complexity of the MOO methods makes their use difficult. In order to achieve the objective of the
158 study presented in this paper, the use of multi-criteria decision aid methods is considered more
159 appropriate as they allow a complete ranking of the thermal renovation solutions.

160 MCDA and MOO methods were often used in the literature for the thermal renovation of buildings.
161 However, they were rarely applied for the thermal renovation of masonry buildings with a heritage
162 value. So far, none of the current methods takes into account at the same times the following
163 aspects:

- 164 • The specificity of the thermal renovation of masonry buildings with a heritage value.
- 165 • A multitude of criteria and thermal renovation solutions, expressed by several decision
166 makers to get a global ranking of the actions.
- 167 • The communication among the decision makers to obtain a consensus regarding the
168 definition of evaluation criteria, and the potential thermal renovation solutions.

- 169 • The difficulty in assessing the weights (importance) of each criterion for each decision
170 maker.
- 171 • Additional constraints such as the maximum budget allocated to the operation.
- 172 • Conflicts and similarities between the criteria and among decision makers for a better
173 understanding of the decision problem.
- 174 • The application of the partial aggregation MCDA methods PROMETHEE.

175 The current paper proposes a new group decision aid method that combines the Delphi method, the
176 Swing method, and the PROMETHEE methods for the thermal renovation of masonry buildings
177 with a heritage value.

178 **2.3 PROMETHEE methods**

179 PROMETHEE methods are outranking methods that use the partial aggregation. They are useful
180 in the case where the number of alternative to rank is finite. These approaches compare the actions
181 pairwise, and under certain conditions check if one of two actions clearly outrank the other or not
182 from these comparisons. They allow a comprehensive ranking of the various alternatives [27].
183 PROMETHEE methods include PROMETHEE II, the GAIA analysis (Graphical Analysis for
184 Interactive Aid), PROMETHEE V (Optimization under constraints), the group decision support
185 system PROMETHEE GDSS, and other extensions.

186 **2.3.1 PROMETHEE II**

187 PROMETHEE II assumes that the decision maker is able to give a weight and a preference function
188 to each criterion. This information is used to compare the actions in order to establish a
189 comprehensive ranking. Furthermore, the GAIA analysis which is a graphical representation of the
190 problem allows a better understanding of conflicts and similarities between the criteria and the
191 performance of each action regarding different criteria [27], this whole process is explained in the
192 methodology section. Macharis et al. [28] provided a comprehensive literature review on the

193 application of the PROMETHEE II method in various areas. It has been used for the environmental
194 management [29-33], hydrology and Water management [34, 35], and energy management [36-
195 39].

196 **2.3.2 PROMETHEE V**

197 PROMETHEE V allows adding additional constraints required by the decision maker, such as the
198 number of alternatives to be selected, the maximum budget allocated to the operation, and
199 incompatibilities between actions. It also argued that many other types of constraints can be added
200 [40]. This method has already been used by Vetschera and de Almeida [41] to solve a portfolio
201 optimization problem. Fontana and Morais [42] used PROMETHEE V to assist decision makers
202 in selecting a set of feasible alternatives for rehabilitating the greatest number of leakage points in
203 a water network.

204 **2.3.3 PROMETHEE GDSS**

205 PROMETHEE GDSS takes into account the preferences of a group decision. First, the decision
206 makers identify different alternatives and different criteria. Then an individual ranking is
207 established for each decision maker through PROMETHEE II. Furthermore, the method brings
208 together the different individual rankings for a global ranking. This ranking takes the preferences
209 of all decision makers into account. Finally, the global GAIA analysis identifies the decision
210 makers that share similar preferences and those in conflict [43].

211 PROMETHEE GDSS has been successfully implemented to solve multi-criteria and multi-
212 decision maker problems in various areas. Tavana et al. [44] applied it for the oil and gas pipeline
213 planning in the Caspian Sea. Behzadian et al. [45] applied PROMETHEE GDSS to rank technical
214 requirement alternatives in line with customer needs during the final stage of the house of quality
215 process. Gonçalves and Belderrain [46] investigated the application of PROMETHEE GDSS and
216 GAIA methods for the performance evaluation in the subsystems of the ITA-SAT satellite project.

217 Turcksin et al. [47] used the combination of the AHP and the PROMETHEE GDSS methods in
218 order to select the most appropriate policy scenario to stimulate a clean vehicle fleet.

219 The advantage of PROMETHEE methods is that they use the partial aggregation. These methods
220 allow taking into account several quantitative and qualitative criteria without having to do any
221 coding or change the indicators. They do not allow compensation between criteria. With
222 PROMETHEE GDSS, it is possible to reach a global ranking of the actions taking into account the
223 preferences of several decision makers. PROMETHEE V allows considering additional
224 constraints. Finally, GAIA analysis provides information on conflicts and similarities between the
225 different criteria and among the decision makers. However, PROMETHEE methods do not pro-
226 vide any specific guidelines to facilitate:

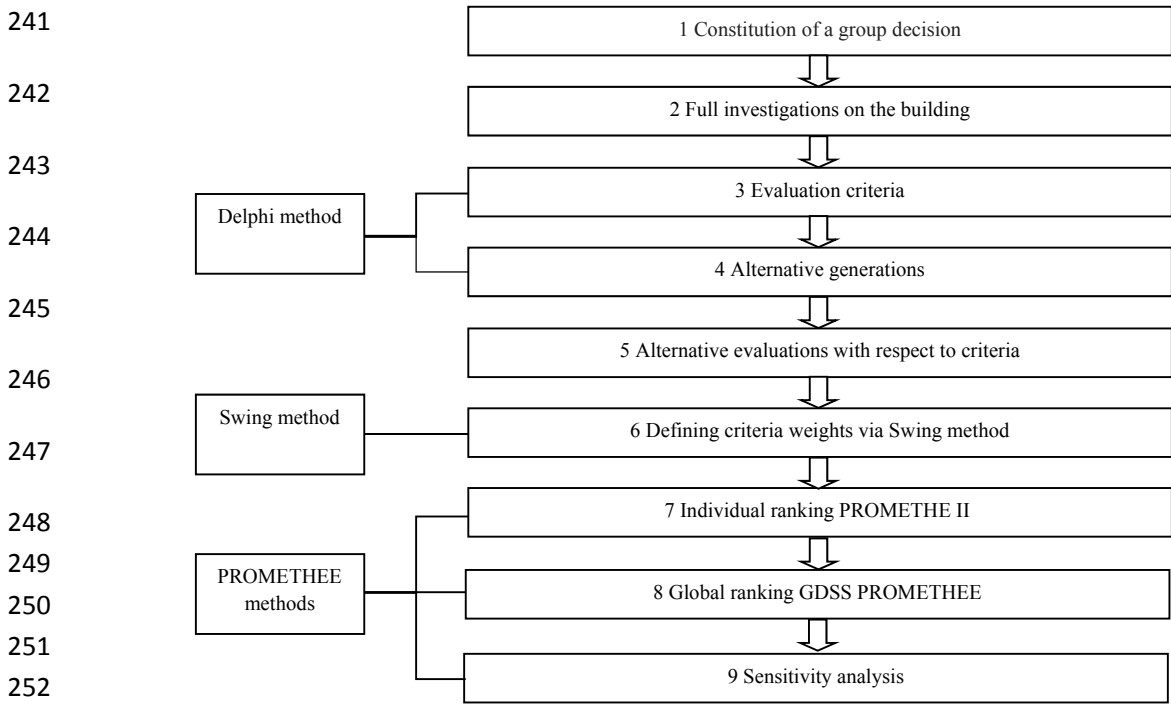
- 227 • The communication among the actors to obtain a consensus regarding the definition of
228 evaluation criteria, and the potential thermal renovation solutions.
- 229 • The assessment of the weights (importance) of the criteria.

230 **3 Methodology**

231 This section presents a new group decision aid method that combines the Delphi method, the Swing
232 method, and the PROMETHEE methods to evaluate different renovation solutions. The method
233 consists of several sequential steps as presented in Figure1: first, the group of decision makers is
234 constituted. After that, the building is investigated, then after through Delphi method the criteria
235 and the thermal renovation solutions are defined. Later with Swing method, each decision maker
236 provides information between the criteria expressed by weights. Finally, the rest of the calculations
237 will be completed using PROMETHEE methods. More details concerning the different steps would
238 be presented in the following subsections.

239

240



254 Figure 1: Proposed methodology to rank different thermal renovation solutions

255

256 **3.1 Constitution of a group decision**

257 The first step is to form a group consisting of the different decision makers involved in the thermal
 258 renovation project (actor concerned with the preservation of buildings, actor concerned by the
 259 reduction of energy consumption, owners, and so on).

260 **3.2 Full investigation on the building**

261 Following the constitution of the decision makers group, a complete documentation of the building
 262 would be performed. This step combines a pre-evaluation of building design plans and
 263 documentation as well as the level 1 audit (walk-through assessment) as demonstrated in Alajmi
 264 [48]. Based on the information collected during the investigation on the building step, each decision
 265 maker can have an idea concerning the potential evaluation criteria and thermal renovation
 266 solutions as argue by Ma et al. [49]. First, in order to familiarise the decision makers with the

267 building in investigation a pre-evaluation of the building plans and documentation, without any
268 visit to the site should be performed. The data collection concerns the following aspect:

- 269 • The implantation of the building and the climate zone.
- 270 • The internal organization (plans, sections).
- 271 • The plan of facades with full details.
- 272 • The area and volume of the building.
- 273 • The methods of construction of the building and the openings (load bearing elements, walls,
274 nature of the connections, roof, floors, and windows type).
- 275 • The energy consumption and the technical equipment's.

276 Later, the group decision should carried out a walk-through assessment, which is the simplest type
277 of audit and the most basic requirement of the energy audit [50]. This level of audit may takes
278 several visits to the building by the group decision makers. The walk-through assessment allows a
279 real evaluation of the current situation of the building, its technical equipment's, and the energy
280 performance of the building. Furthermore, an interview with the building's users would provide a
281 better understanding concerning the building exploitation (the number of occupants, the occupancy
282 scenario and patens, the calculation set point temperature for the heating needs and for the cooling
283 requirements, windows opening hours).

284 **3.3 Evaluation criteria**

285 The thermal renovation solutions should be evaluated on a multiple criteria basis. The definition
286 of the evaluation criteria would be accomplished by the Delphi method, which is a structured group
287 interaction method that works through multiple rounds of opinion collections and anonymous
288 feedback. It is a useful tool to obtain a consensus of opinions from a group about an issue not
289 subject to objective solution. Keeney et al. [51] have provided excellent review of the Delphi
290 method and its applications. First using interviews, individual lists of criteria are obtained; each

291 decision maker is asked individually to express their evaluation criteria, taking into accounts
292 different aspects such as: economic, environmental, cultural, and architectural. The criteria can be
293 for example: investment cost, energy consumption decrease, and so on. Secondly, all the individual
294 lists will be combined to form a complete list, which is shared with all decision-makers. They are
295 invited to review this information and to revise and resubmit their initial individual list. This
296 process is repeated until the participants decide that they cannot reduce further the number of
297 criteria in the list. Tavana et al. [44] have already combined Delphi method with PROMETHEE
298 methods. The association of the Delphi method with PROMETHEE method allows improving the
299 communication among the decision makers. It also facilitates the process of the definition of
300 evaluation criteria and the thermal renovation solutions.

301 **3.4 Alternative generations:**

302 Once the investigation on the building is completed and the evaluation criteria are defined, the
303 group decision should formulate thermal renovation alternatives. The thermal renovation solutions
304 will take into account only the common area, and will concern only the insulation of the building
305 envelope (external roof insulation, external wall insulation, and so on). This step can be performed
306 with an open discussion among decision makers or through the same process used for the
307 evaluation criteria selection.

308 **3.5 Evaluation of the alternatives in terms of the criteria:**

309 Each alternative should be evaluated in terms of all the criteria. These evaluations can be
310 quantitative (obtained from thermal dynamic simulation tool, accounting calculations etc) or
311 qualitative (expert judgments, interviews, and so on).

312 **3.6 Defining criteria weights via Swing method:**

313 According to PROMETHEE theory, each decision maker should provide information between the
314 different criteria expressed by weights (w_j). They represent the importance of each criterion for the

315 decision maker. However, PROMETHEE methods do not provide any specific technique to define
 316 the weights of the criteria. In the literature, the Analytical Hierarchy Process (AHP) method was
 317 often combined with PROMETHEE method to help the decision makers to assign weights to the
 318 criteria [52]. However, AHP method requires importance ratio judgments between each pair of
 319 criteria and the complexity of this method makes its implementation quite inconvenient. In this
 320 paper, the Swing method has been used to determine the weights of the criteria. The Swing method
 321 uses a reference state in which all criteria are at their worst level, and asks the interviewee to assign
 322 points to states in which one criteria at a time moves to the best state. The weights are then
 323 proportional to these points. The advantages of the Swing method are that it is fairly fast and
 324 interviewees readily give answers. It only requires knowing the criteria ranges. On the other hand,
 325 the disadvantages are that the technique is based on direct rating, it does not include consistency
 326 checks, and the extreme outcomes to be compared may not correspond to a realistic alternative
 327 [53]. Combining Swing method with PROMETHEE methods allow simplifying the determination
 328 of the criteria weights. So far, the association of these two methods has not been performed in multi
 329 criteria decision literature.

330 **3.7 Individual ranking PROMETHEE II**

331 In this step, each decision maker should provide information within the same criterion expressed
 332 by preference functions ($P_j(a,b)$). They represent for each pair of alternatives “ a ”, “ b ” the
 333 preference intensity of “ a ” over “ b ”. A multi-criteria preference index is defined as in equation
 334 (1).

$$\pi(a, b) = \sum_{j=1}^k w_j \times P_j(a, b) \quad (1)$$

335 Where $\pi(a, b)$, expresses the preference degree of “ a ” over “ b ” regarding all the criteria, it varies
 336 from 0 to 1.

337 Where w_j , is the normalized weight assigned to criterion j

338

339 The facilitator would help the decision-makers to choose their preference functions. There are six
340 different types of criterion according to their preference functions [54]. In addition, decision
341 makers should specify the threshold values p (strict preference threshold when the difference
342 between two actions “ a ” and “ b ” is very strong and very important to the decision maker) and q
343 (indifference threshold when the difference between the actions “ a ” and “ b ” is insignificant).

344 The weights and the preference functions of the decision makers will be used to compare the
345 actions. First, the leaving flow and the entering flow have to be calculated:

346 The leaving flow $\Phi^+(a)$ represents a strength measure. It is a number between 0 and 1; this
347 means that for a given action, if the leaving flow is 1, the action is preferable to all the others
348 actions on all the criteria, and if the leaving flow is equal to 0, this means that the action does not
349 represent any advantage over the other actions. Φ^+ is calculated with equation (2).

$$\Phi^+(a) = \frac{1}{n-1} \sum_{b \neq a} \pi(a, b) \quad (2)$$

350 The entering flow $\Phi^-(a)$ represents a weakness measure. It is a number between 0 and 1, where
351 0 is the best solution and 1 the worst one. Φ^- is calculated with equation (3).

$$\Phi^-(a) = \frac{1}{n-1} \sum_{b \neq a} \pi(a, b) \quad (3)$$

352 Secondly, we calculate the net flow $\Phi(a)$. It represents the difference between the two flows as
353 shown in equation (4). The net flow allows establishing a comprehensive ranking of actions. Then
354 the decision problem could be illustrated through the GAIA analysis (Graphical Analysis for
355 Interactive Aid). It allows a better understanding of conflicts and similarities between the criteria
356 and the performance of each action regarding different criteria.

$$\phi(a) = \phi^+(a) - \phi^-(a) \quad (4)$$

357 Additional constraints can be introduced according to the requirements of the decision makers
 358 through PROMETHEE V. A binary variable (0-1) x_i is associated with each action “ a_i ”: $x_i = 1$
 359 means that the action “ a_i ” is selected, $x_i = 0$ means it is not. The aim is to select the actions so that
 360 the sum of the Phi (ϕ) of these actions is maximum as shown in equation (5).

$$\max \sum_{i=1}^n \phi(a_i)x_i \quad (5)$$

361

362 **3.8 Global ranking: GDSS PROMETHEE**

363 The global net flow of the group decision can be obtained directly by the weighted sum of the
 364 individual flows equation (6). The global flow for a given alternative is express as follows:

$$\phi_g(a) = \sum_{s=1}^s w_s \phi^s(a) \quad (6)$$

365 Where w_s is the normalized weight assigned to each DMs

366 The global net flows provide directly the PROMETHEE GDSS ranking of the alternatives
 367 following the group decision preferences. Additional constraints can be added through
 368 PROMETHEE V as well. Later the global GAIA analysis is used for the global ranking. It
 369 contributes to understand the preferences of the different decision makers.

370 **3.9 Sensitivity analysis**

371 First, the effect of changing the criteria weights on the rank of the thermal renovation solutions for
 372 each decision maker should be analysed. Secondly, the effect of changing the weights of the
 373 decision makers on the global ranking should be studied as well.

374

375

376 **4 Case study :**

377 In this section, a case study is presented. It is the building number 11 Boulevard Matta, Oran,
378 Algeria. It is a neoclassical colonial collective building, constructed in masonry between the late
379 19th century and early 20th century (see Figure 2). The aim of this case study was to test the
380 applicability of the method in the thermal renovation of masonry buildings.



381

Figure 2: Neoclassical colonial collective building constructed in masonry

382

383 **4.1 Decision context definition**

384 Fours (DM) participated in this study. Although, the group members were not selected by
385 ourselves. We contacted by phone and emails the stakeholders concerned about the thermal
386 renovation. Following this, each stakeholder appointed a representative to express their interests
387 and point of views. DM1 was a representative of the national agency for the promotion and the
388 rationalization of the energy use (APRUE), an agency in charge of the energy consumption
389 reduction in the residential sector in Algeria. DM 2 represented the department of urban planning
390 and construction (DUC), a national department in charge of masonry buildings' preservation in
391 Algeria. DM3 was the representative of all the building's users selected by themselves. DM4 was
392 an expert from a private expert firm in the thermal renovation of masonry buildings, which has
393 been selected by the government to undertake the refurbishment of these specific buildings.

394 **4.2 Case study investigation**

395 The group decision makers have conducted a pre-evaluation of the building design plans and
396 documentation as well as the level 1 audit (Walk-through assessment) as indicated in subsection
397 3.2. The total building volume is 2,320 m³. The floor- area is 580 m². The building has four flats
398 occupied by four different family. Concerning the scenario occupation, there is at least one person
399 occupying each flat for almost all the times. The annual energy consumption for heating and
400 cooling of the building is about 66,332 kWh. The building is equipped with a collective heating
401 system and four individual air conditioning systems. The building does not have any mechanic
402 ventilation and is ventilated naturally. The set point temperature for the heating system is 21 ° C,
403 and 26 ° C for the cooling systems. The Exterior masonry walls have a thickness of 55 cm and a
404 U-value of 1.19 W/m²K. The roof is built in vaulted brick floor and metal beams; it has a U-value
405 of 1.69 W/m²K. The windows are all single glazed with a U value 5.68 W/m²K. The roof, walls,
406 and widows are not damaged. However, they are not insulated which consequently make the
407 building consumes more energy. The main façade is well conserved. It presents historic aesthetic
408 features while the secondary and courtyard facades as well as the roof does not present such
409 features

410 **4.3 Evaluation criteria**

411 The Delphi technique is used to gather input from those 4 DM without requiring them to work face
412 to face. We used semi structured interview to gather information, obtain feedback and make
413 conclusions. In the first Delphi round, the DMs were asked individually to consider the economic,
414 energetic, environmental, architectural, social, and technological issues and to compile and explain
415 a set of criteria considered to be important in the thermal renovation project. These personal lists
416 were provided to the facilitators anonymously. Then, the facilitators combined all of these criteria
417 into a list of 11 criteria as indicated in table 1. In round 2, this list was shared with all the DMs.
418 They are invited to review this information, to revise, and resubmit their initial individual list. The

419 facilitators combined all of these criteria into a new list of 7 criteria as shown in table 1. Again, in
 420 round 3, the synthesized list of criteria from round 2 was shared with all the DMs, and they were
 421 asked to revise and resubmit their individual list from round 2. The facilitators then combined all
 422 of these criteria into another new list with 4 criteria. At this point, the DMs agreed that they could
 423 not reduce further the number of criteria in the list. Consequently, a decision was made to use the
 424 4 evaluation criteria (the energy consumption, the investment cost, the risk of the loss of building
 425 historic aesthetic features and the risk of the fabric) obtained from round 3 as presented in table 1.
 426

Rounds	Criteria code	Classification	Criteria
Round 1	1	Economic	Investment cost
	2	Economic	Payback period
	3	Technological	Availability of Manpower
	4	Technological	Availability of materials
	5	Energetic	Energy consumption decrease
	6	Environmental	Decrease of CO2 emissions
	7	Architectural	Risk of the fabric decay
	8	Architectural	Risk of the loss of building historic aesthetic features
	9	Social	Summer comfort
	10	Social	Inconvenience caused by the thermal renovation
	11	Social	Duration of the thermal renovation work
Round 2	1	Economic	Investment cost
	2	Economic	Payback period
	5	Energetic	Energy consumption decrease
	6	Environmental	Decrease of CO2 emissions
	7	Architectural	Risk of the fabric decay
	8	Architectural	Risk of the loss of building historic aesthetic features
	9	Social	Duration of renovation work
Round 3	1	Economic	Investment cost
	5	Energetic	Energy consumption decrease
	7	Architectural	Risk of the fabric decay
	8	Architectural	Risk of the loss of building historic aesthetic features

427

428

Table 1: Selection of evaluation criteria through Delphi method

429

The evaluation indicators were chosen in such way that they could be easily understood by the
 430 group decision. The energy consumption was expressed with the heating and air conditioning
 431 annual need decrease. This evaluation was done under TRANSYS [55], which is a dynamic thermal
 432 simulation software. The investment cost was expressed in Algerian dinars (converted in this paper

433 to US dollar). It included the supply costs and the labour. The risk of the loss of building historic
434 aesthetic features was evaluated by means of subjective judgments and expressed in qualitative
435 scale (see Table 2). The risk of the fabric decay in the walls is due to moisture accumulation, which
436 might happen when additional thermal renovation solutions are not adapted to the masonry building
437 [10]. In this research all thermal renovation alternatives were evaluated in terms of moisture
438 accumulation under the WUFI (Wärme Und Feuchte Instationär—which, translated, means heat
439 and moisture transiency) software [56], WUFI allows the simulation of heat and mass transfer in
440 walls [57]. According to the result, the risk of fabric decay of each solution was expressed by
441 qualitative scale (see Table 2).

Scale	Risk level
1	Very low
2	Low
3	Medium
4	High
5	Very high

442

Table 2: Qualitative scale for risks evaluation

443

444 **4.4 Alternative evaluation:**

445 Still using the Delphi method, DM1, DM2 and DM4 generated thermal renovation alternatives.

446 The thermal renovation solutions took into account only the common area, and concerned only the

447 insulation of the building envelope (see Table 3).

448

449

450

451 **4.5 Evaluation of the alternatives in terms of the criteria**

452 Table 3 shows the evaluation of all the alternatives in term of the selected criteria.

Codes	Actions (thermal renovation solutions)	C1	C2	C3	C4
		KWh	US dollar	Qualitative	Qualitative
A1	Exterior insulation of the main facade with 10 cm of expanded polystyrene	6675	1611	Very high	Very high
A2	Exterior insulation of the main facade with 10 cm of cellular concrete	6296	2255	Very high	Low
A3	Exterior insulation of the main facade with 10 cm of wood fiber	6384	1772	Very high	Low
A4	Exterior insulation of the main facade with 6 cm of lime hemp plaster	4062	1933	Very low	Very low
A5	Exterior insulation of the secondary facade and courtyard with 10 cm of expanded polystyrene	5461	1295	Medium	Very high
A6	Exterior insulation of the secondary facade and courtyard with 10 cm of cellular concrete	5155	1813	Medium	Low
A7	Exterior insulation of the secondary facade and courtyard with 10 cm of wood fiber	5223	1424	Medium	Low
A8	Exterior insulation of the secondary facade and courtyard with 6 cm of lime hemp plaster	3482	1554	Very Low	Very Low
A9	Exterior insulation of the roof with 10 cm of expanded polystyrene	8918	2669	Very low	Low
A10	Exterior insulation of the roof with 10 cm of wood fiber	8623	2936	Very low	Low
A11	Exterior insulation of the roof with 15 cm of expanded polystyrene	9897	4004	Very low	Low
A12	Exterior insulation of the roof with 15 cm of wood fiber	9618	4271	Very low	Low
A13	Double glazing window installation.	12188	7330	Medium	-
A14	Double windows installation	11027	7521	Very low	-
A15	Secondary glazing installation	5200	2255	Very low	

453 C1: Energy consumption decrease; C2: Investment cost; C3: Risk of the loss of building historic aesthetic features,
 454 C4: Risk of the fabric decay

455

Table 3: Evaluation table

456

457

458 **4.6 Defining criteria weigh via Swing method**

459 The weights of the criteria were defined through SWING method using a reference state where all
 460 criteria were at their lowest level. Each decision maker was asked which criterion he would
 461 improve to the highest level, assuming that only one criterion could be improved. The next step
 462 consisted in asking the decision maker to give a value to (e.g. in the range 0–100) to this swing in
 463 terms of importance. The score 100 represented the maximum importance. Finally, the scores were
 464 normalized to sum up to one to get the criteria weights. The weight of DM3 represented the average
 465 weight of all building users (see Table 4). DM1 and DM3 considered the criteria investment cost
 466 and energy consumption decrease as very important. While the criteria risk of the loss of building
 467 historic aesthetic features and the risk of the fabric decay were less important. For DM2, the criteria
 468 risk of the loss of building historic aesthetic features and the risk of the fabric decay were
 469 respectively very important. Whilst the criteria energy consumption decrease and investment cost
 470 were less important. For DM4 the criteria risk of fabric decay, risk of the loss of building historic
 471 aesthetic features, energy consumption decreases were respectively important. The investment cost
 472 was less important.

473

Criteria		C1	C2	C3	C4
DM1	Weight	0.279	0.264	0.220	0.235
	Preference	Usual	Usual	Level q=1 p=2	Level q=1 p=2
DM2	Weight	0.235	0.220	0.279	0.264
	Preference function	Usual	Usual	Usual	Usual
DM3	Weight	0.275	0.284	0.226	0.213
	Preference function	Usual	Usual	Level q=1 p=2	Level q=1 p=2
DM4	Weight	0.262	0.205	0.264	0.269

Preference function	Usual	Usual	Level q=1 p=2	Level q=1 p=2
---------------------	-------	-------	---------------------	---------------------

474 C1: Energy consumption decrease; C2: Investment cost; C3: Risk of the loss of building historic aesthetic features,
 475 C4: Risk of the fabric decay, q represents the indifference threshold and p represents the preference threshold.
 476

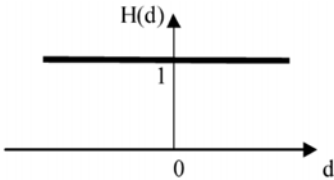
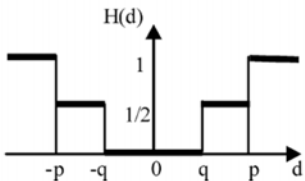
477 Table 4: Weights, preference functions, threshold parameters evaluated per decision-makers

478

479 **4.7 Individual ranking PROMETHEE II and analysis**

480 According to PROMETHEE theory, each decision maker has provided information within the same
 481 criterion expressed by preference functions (Pj(a,b)). The preference functions type I, and types IV
 482 (see Table 4 and Table 5) were chosen by the decision makers.

483

Generalized criterion type	Preference functions ($H(d)$), $d = g_j(a) - g_j(b)$
Type I: Usual criterion. $H(d) = \begin{cases} 0 & \text{if } d = 0 \\ 1 & \text{if } d \neq 0 \end{cases}$	 <p>None</p>
Type IV: Level criterion (best suited for qualitative criteria) $H(d) = \begin{cases} 0 & \text{if } d \leq q \\ \frac{1}{2} & \text{if } q < d \leq p \\ 1 & \text{if } p < d \end{cases}$	 <p>q,p</p>

484 $g_j(a)$ is the performance of alternative “a” in criterion “j”. “q” represents the indifference threshold
 485 and “p” represents the preference threshold.
 486

487 Table 5: The shapes of the two preference functions used in this paper adapted from Vincke and
 488 Mareschal [54]

489 Under Visual PROMETHEE software [58] it was possible to get an individual ranking
 490 PROMETHE II for each decision maker (see Table 6). For this purpose, three additional constraints
 491 (number of actions to select, incompatibilities between actions, maximum budget available) were
 492 added since there were 15 alternatives and only 4 could have been selected simultaneously, the
 493 maximum budget available was about 16.000 US dollar. These constraints were taken into account
 494 through PROMETHEE V method.

495 The constraint of the number of actions to select is indicated in equation (7).

$$\sum_{i=1}^n x_i = 4 \quad (7)$$

496 Where 4, represents the number of actions to select, and x_i is a binary variable (0-1) associated to
 497 each action a_i : $x_i = 1$ means that action a_i is selected while $x_i = 0$ means it is not.

498 The constraints of the incompatibilities between actions (A) are indicated in equation (8, 9, 10, and
 499 11).

$$A1 + A2 + A3 + A4 = 1 \quad (8)$$

$$A5 + A6 + A7 + A8 = 1 \quad (9)$$

$$A9 + A10 + A11 + A12 = 1 \quad (10)$$

$$A13 + A14 + A15 = 1 \quad (11)$$

500 The constraint of the maximum budget available is expressed in equation 12

$$\sum_{i=1}^n b_i \times x_i \leq 16.000 \quad (12)$$

501 Where the number 16.000 represents the maximum budget available (in US dollar), and b_i
 502 corresponds to the investment cost of each action a_i .

Ranking	DM1	DM2	DM3	DM4
1	A7	A8	A7	A7
2	A11	A11	A9	A11
3	A13	A4	A13	A13
4	A3	A14	A3	A4

503

504

Table 6: Individual PROMETHEE II ranking with additional constraints

505

506

Table 6 shows that the ranking of the thermal renovation solutions was different for all decision

507

makers. DM1 and DM3 provided almost a similar ranking. The only difference is that for DM3 A9

508

is preferable to A11. A3 was selected by both of DM1 and DM3, this action represents very high

509

risk of loss of building historic aesthetic features, which shows that DM1 and DM3 do not give

510

enough importance to this criterion. DM4 provided a ranking close to DM1 with A7, A11, and A13

511

in the top row. The difference is that A4 is preferred to A3. DM4 has almost succeeded to balance

512

between all the criteria. DM2 had a completely different ranking from the previous decision

513

makers. A8, A4, and A14 had very weak performance on the energy consumption decrease and the

514

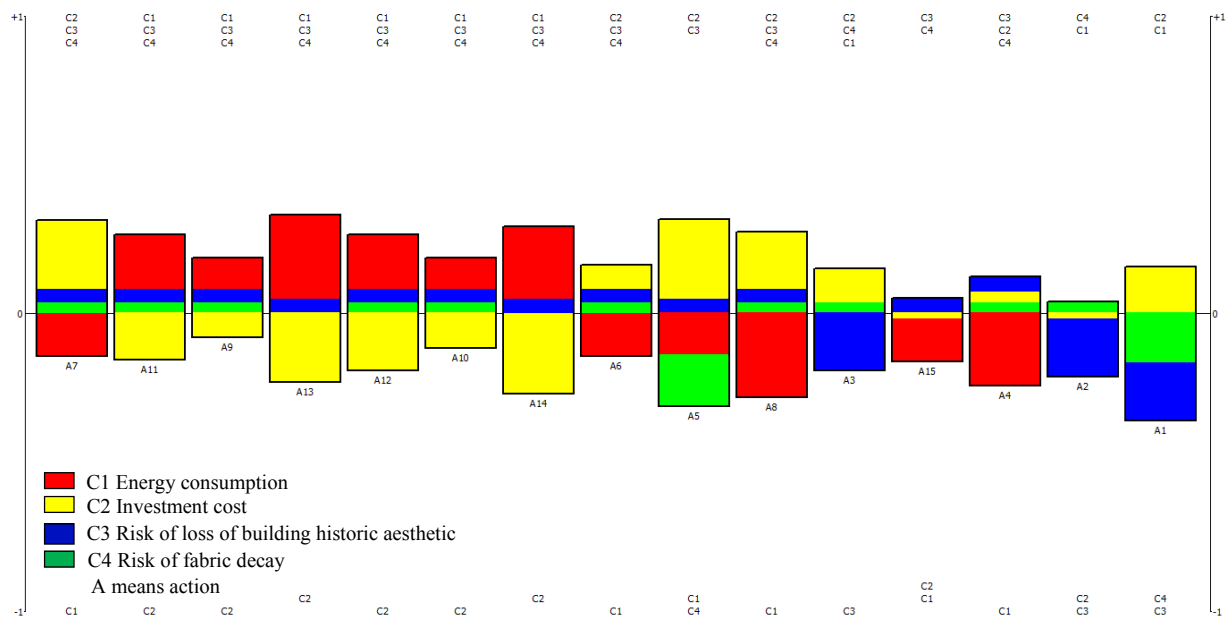
investment cost, which shows that DM2 does not give enough importance to those two criteria. He

515

cares only about the risk of fabric decay and the risk of the loss of building historic aesthetic

516

features.



517

518

Figure 3: Details of the phi net flow computation for DM1

519

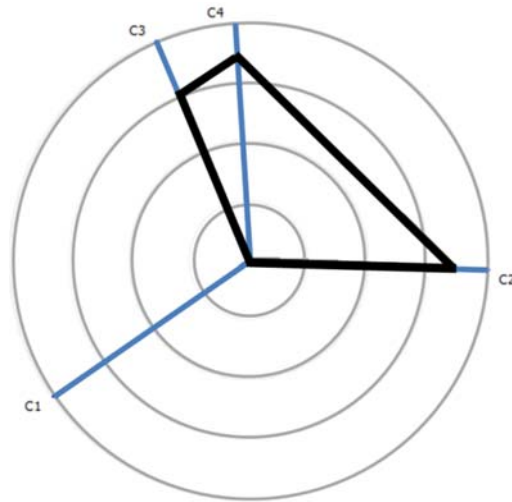
520 For example Figure 3 shows the detail of the Phi net flow computation for DM1, highlighting the
 521 good and weak characteristics of each action. For each action, a bar was drawn. The different parts
 522 of each bar were coloured according to the colour coding of the criteria. Each part is equivalent to
 523 the influence of one criterion to the phi net flow score of the action. Positive (upward) parts
 524 correspond to good characteristics, while negative (downward) parts correspond to weaknesses.
 525 The balance between positive and negative slices is equal to the phi score. Actions were ranked
 526 from left to right according to the PROMETHEE II Complete Ranking (without the additional
 527 constraints).

528 For DM1, the actions A7, A11, A13, and A3 were preferable to all the other actions (see Table 5)
 529 .The exterior insulation of the secondary facade and courtyard with 10 cm of wood fiber (A7) had
 530 very good features in the investment cost (C2), good features in the risk of the loss of building
 531 historic aesthetic features (C3) and the risk of fabric decay (C4), however it had weak features in
 532 the energy consumption decrease (C1). The exterior insulation of the roof with 15 cm of expanded

533 polystyrene (A11) and the double glazing window installation (A13) both had very good features
534 in the energy consumption (C1). They had good features in the risk of the loss of building historic
535 aesthetic features (C3). They had very weak features in the investment cost (C2). The exterior
536 insulation of the main facade with 10 cm of wood fiber (A3) had very good features in the
537 investment cost (C2). It had medium features in the energy consumption decrease (C1). It had low
538 risk of fabric decay (C4). It had very weak features in the risk of the loss of building historic
539 aesthetic features (C3).

540 Based on the above ranking of DM1, (A7) was the best action despite the fact that it has weak
541 features in the most important criteria for DM1 (energy consumption decrease). This implies that
542 the best thermal renovation solutions are not those that have the best performance in the criteria
543 with the highest weight, but they are those that represent the best compromise.

544 Then the GAIA Web was drawn to illustrate conflicts and similarities between the criteria for each
545 decision maker. Furthermore, it allows understanding the performance of each action concerning
546 the different criteria. The GAIA Web shows a graphical representation of the unicriterion net flow
547 scores for a selected action. The criteria vectors (blue colour) which express the same preferences
548 have similar orientation while conflicting criteria have opposite direction. For each criterion, the
549 radial distance corresponds to the net flow score (-1 at the center and +1 on the outer circle). For
550 example, Figure 4 shows the GAIA web for DM2 when action A8 is selected. The exterior
551 insulation of the secondary facade and courtyard with 6 cm of lime hemp plaster (A8) had very
552 good features in the investment cost, in the risk of the loss of building historic aesthetic features
553 and in the risk of fabric decay. However, it had very weak features in the energy consumption
554 decrease. The criteria risk of the loss of building historic aesthetic features and risk of fabric decay
555 almost share the same orientation and express similar preferences. The criteria investment cost and
556 energy consumption decrease have opposite orientation and express conflicting preferences.



557

558 C1: Energy consumption decrease; C2: Investment cost; C3: Risk of the loss of building historic aesthetic features,
 559 C4: Risk of the fabric decay

560

561 Figure 4: GAIA web for DM2 when action A8 is selected

562 **4.8 Global ranking PROMETHEE GDSS and analysis**

563 The net flow of the 4 decision makers (DM) were collected together in a global decision matrix as
 564 indicated on Table 7.

Action	DM1	DM2	DM3	DM4
	Net flow	Net flow	Net flow	Net flow
A1	-0.205	-0.302	-0.183	-0.308
A2	-0.174	-0.255	-0.183	-0.201
A3	-0.042	-0.145	-0.041	-0.098
A4	-0.12	0.158	-0.116	-0.088
A5	0.004	-0.185	0.043	-0.062
A6	0.016	-0.154	0.022	0.03
A7	0.168	-0.028	0.185	0.148
A8	-0.009	0.251	0.007	-0.006
A9	0.105	0.16	0.095	0.127
A10	0.067	0.129	0.055	0.097
A11	0.109	0.164	0.093	0.139
A12	0.071	0.133	0.052	0.11
A13	0.099	-0.053	0.079	0.13
A14	0.022	0.12	0	0.065
A15	-0.111	0.006	-0.109	-0.083

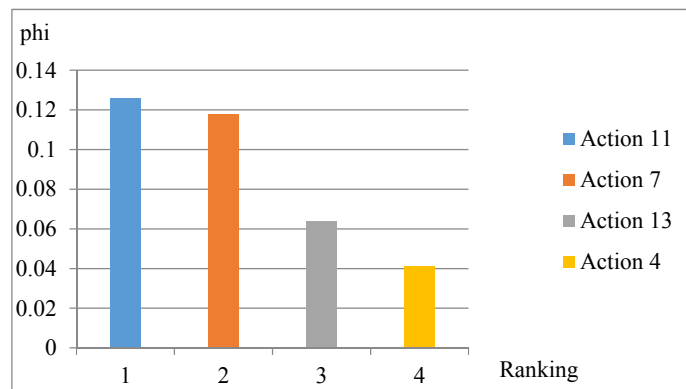
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Table 7: Global decision matrix

567 A PROMETHEE GDSS global ranking was performed. The same constraints used in the individual
568 ranking were introduced through PROMETHEE V. According to Macharis et al. [43], all the
569 decision-makers had the same relative importance (the same weights, DM1 0.25, DM2 0.25, DM3
570 0.25, DM4 0.25). From the group decision viewpoint, the actions A11, A7, A13 and A4 are
571 respectively preferable to all the other actions (see Figure 5).

572



573

574

575 Where phi is the global net flow of the group decision for each action.

576

577 Figure 5: Global ranking PROMETHEE GDSS under constraints

578

578 The decision problem was then represented using the GAIA plan (see Figure 6), it provides help to
579 understand the different decision makers' preferences and the performance of each action for them.

580 The GAIA plan is the result of principal component analysis, and it preserves the highest possible
581 amount of information after the projection. The projection of 4 dimensional spaces of the criteria

582 in a two dimensional plane preserved 97.4% the total data. The Information provided in this paper
583 by the GAIA plan is considered reliable since their value is greater than 80% as explained by

584 Figueira, J et al. [59]. The length of decision axis (red axis) is a force measure for the differentiation
585 between two alternatives. The alternatives are presented by dots. The actions with the same colour

586 cannot be selected simultaneously. The decision makers are represented by vectors. The decision

587 makers who share the same preferences have similar orientation while those with conflicting
588 preferences have different directions.

589 The actions A11, A9, A7, A12, A10, and A13 are the closest from the direction of the decision axis
590 so they represent the best alternatives. The actions A8, A14, A6, and A4 are less preferable and
591 more distant from the direction of the decision axis. The actions A5, A15, A3, A2, and A1 are the
592 least preferable and the furthest from the direction of the decision axis. The vectors of DM1 and
593 DM3 share the same orientation so they have similar preferences. The vector of DM4 has almost
594 the same direction of DM1 and DM3. However, the vector of DM2 has a completely different
595 direction from the others. Consequently, DM2 has very different preferences compare to DM1,
596 DM3, and DM4. This clarifies why DM1, DM3, and DM4 had less or more a similar individual
597 ranking while DM2 had a completely different individual ranking.

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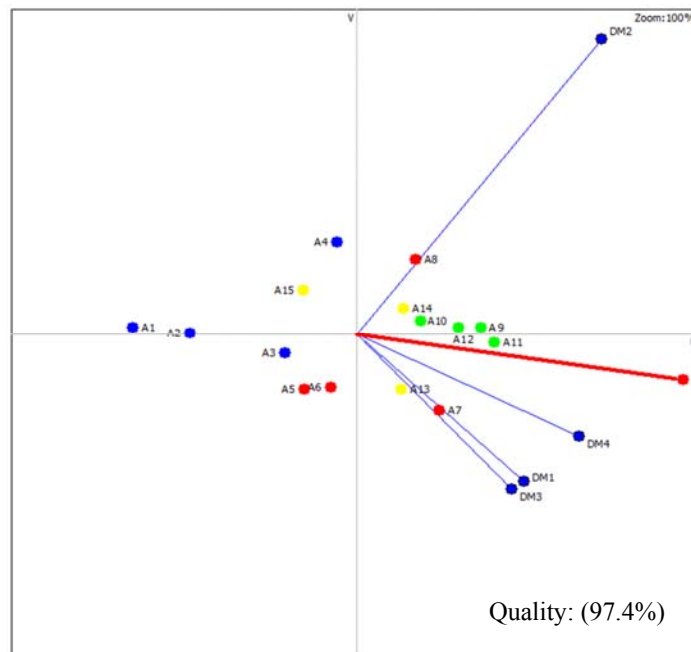
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Figure 6: Global GAIA plane

612 **4.9 Sensitivity Analysis**

613 PROMETHEE method involves the determination of subjective parameters (criteria weights,
 614 decision maker’s weights) [27]. It is interesting to investigate the influence they have on the
 615 rankings when deviations in their values are introduced. First, an analysis was done about how
 616 changing the weights assigned to the criteria could affect the rank of the selected thermal renovation
 617 solutions for each decision maker. This analysis was performed through the investigation of the
 618 weight stability intervals under visual PROMETHEE software [58]. The weight stability intervals
 619 give the limits for each criterion where variations of the criterion weight in term of percentage
 620 would not alter the individual PROMETHEE ranking of the thermal renovation solutions.
 621 Table 8 shows the weight stability intervals in percentage terms of all the criteria for each decision
 622 maker (DM). Hence, changing the weight of energy consumption decrease within the interval
 623 [27%, 30%] would not affect the rank of the selected alternatives for DM1. Similarly, modifying
 624 the weights of the risk of the loss of building historic aesthetic features between 10 and 99 % will
 625 not change the rankings for DM2. It can be noted that the information provided by the stability
 626 intervals applies only when the weights are modified singly.

Criteria	DM1		DM2		DM3		DM4	
	% weight stability intervals		% weight stability intervals		% weight stability intervals		% weight stability intervals	
	Min	Max	Min	Max	Min	Max	Min	Max
C1	27	30	22	27	21	28	22	26
C2	24	28	20	22	28	34	21	23
C3	10	29	10	99	13	27	26	99
C4	19	62	23	27	12	57	23	71

627
 628
 629

Table 8: Weight stability intervals of the criteria

630 Secondly, the stability of the ranking of the selected solutions from the group decision view point
 631 was analysed by a final sensitivity analysis (see Table 9). In this analysis, the weight stability
 632 intervals give the limits for each decision maker where variations of the decision maker's weights
 633 in term of percentage would not alter the group decision ranking PORMETHEE GDSS of the
 634 thermal renovation solutions. The final sensitivity analysis reveals that changing the weight from
 635 [12%, 50%] for DM1, [12 %, 51%] for DM3, [22 %, 49%] in DM2, and [8 %, 62%] for DM4
 636 would not affect the global ranking of the thermal renovation solutions, which is a large range of
 637 variation. The sensitivity analysis revealed that considerable changes in decision maker's weights
 638 would not affect the global ranking; this proves that the proposed method is robust with respect to
 639 the different decision maker's preferences.

640

Decision maker	% Weight of decision maker	% Weight stability intervals	
		Min	Max
DM1	25	12	50
DM2	25	22	49
DM3	25	12	51
DM4	25	8	62

641

642

643

Table 9 Weight stability intervals of the DMs

644 **5 Evaluation of the method**

645 The proposed method considers each thermal renovation of masonry building project as a unique,
 646 with its own context, actors, specificity and patrimonial value. The method does not aim to define
 647 standard evaluation criteria or thermal renovation solutions as proposed in [8-10], but it offers a
 648 logical approach to determinate the most relevant criteria according to a specific context and to
 649 rank the best thermal renovation solutions.

650 The MCDA approaches used for the thermal renovation considered only the preferences of building
651 users by either interviews [20] or questionnaires methods [21]. However, the proposed method
652 takes the preferences of several stakeholders into account (actor concerned with the preservation
653 of buildings, actor concerned by the reduction of energy consumption, building users, expert). It
654 uses the Delphi method to improve the communication among the decision makers and help them
655 to obtain a consensus regarding the definition of evaluation criteria and thermal renovation
656 solutions. The selected criteria in this paper were considered as relevant as they satisfied the general
657 requirements listed by Keeney et al. [51].

658 Concerning the weight elicitation, the Swing method was effective to simplify the process of the
659 determination of the criteria weights. The interview questions were clearly presented as confirmed
660 by the respondents, which agrees with Ferretti et al. [60]. However, according to the case study in
661 this paper, the Swing method seems to be not suitable when a respondent expresses uncertainties
662 and vagueness in judgments. To the best of our knowledge, the paper extends the literature in multi-
663 criteria decision analysis as the Swing method has not been combined with the PROMETHEE
664 methods before.

665 Most of the MCDA applied in the thermal renovation literature uses the complete aggregation
666 approach or the partial aggregation methods ELECTRE. So far, the partial aggregation method
667 PROMETHEE GDSS group decision has not been used in this area. The main contribution of the
668 proposed method is to use PROMETHEE GDSS. The method takes into account the preferences
669 of different decision makers in order to get a global ranking of the thermal renovation solutions.
670 Furthermore, it allows taking into account several quantitative and qualitative criteria without
671 having to do any coding contrary to the other methods reviewed in the literature [9, 10, 17-21]
672 where it is necessary to carry out coding. In addition, the proposed method does not allow the
673 compensation between criteria. Indeed, the result shows that the best thermal renovation solutions

674 are not those that have the best performance in the criteria with the highest weight but those which
675 represent the best consensus, this agrees with Macharis et al. [27].

676 The method offers the possibility to introduce additional constraint through PROMETHEE V. This
677 feature is very useful for real life problems when the number of actions or the available budget is
678 limited according to Brans [40]. The method provides completely innovative features in the thermal
679 renovation literature; it uses the GAIA analysis for a better understanding of the conflicts and
680 similarities between the criteria and among decision makers. Furthermore, it helps to solve conflicts
681 between decision makers as indicated by Macharis et al. [43].

682 The method has been implemented with a real team and real data for a planned project. It has been
683 validated by the decisions makers. Although, a debate among the decision makers took place to
684 finalise and digest the outcome of the proposed method. They all considered the selected criteria
685 as relevant. Furthermore, the global ranking was accepted by all the decision makers, they all
686 agreed that the selected thermal renovation solutions represent the best consensus to balance
687 between all the criteria. In addition, the results have also been validated through a sensitivity
688 analysis. It has been checked that the solutions found were stable and were not influenced by the
689 decision-maker preferences. However, it should be noticed that the thermal renovation solutions
690 were not implemented yet. The method described in this article is universal, and can always be
691 applied for selecting thermal renovation solutions when masonry buildings are considered.

692 **6 Conclusions**

693 The paper has an innovative value due to the proposal of a new group decision aid method in both
694 multi-criteria decision and thermal renovation of masonry buildings literature. The proposed
695 method combines the Delphi method, the Swing method, and the PROMETHEE methods. The aim
696 of the proposed method is to rank different thermal renovation solutions using multi-criteria and
697 multi-decision makers approach. A case study was presented to test the applicability of the method
698 in the thermal renovation of masonry buildings. The results showed that it was possible to get a

699 full ranking of the renovation solutions. The Delphi method was effective to select the relevant
700 criteria and the potential thermal renovation solutions. From the group decision viewpoint, the
701 relevant criteria were the energy consumption decrease, the investment cost, the risk of the loss of
702 building historic aesthetic features, and the risk of fabric decay. The Swing method simplified the
703 pro-cess of the determination of the criteria weights. The PROMETHEE methods provided the best
704 consensus between the decision makers. The best solutions were respectively the exterior insulation
705 of the roof with 15 cm of expanded polystyrene, the exterior insulation of the secondary facade and
706 courtyard with 10 cm of wood fiber, and the double-glazing window installation and the exterior
707 insulation of the main facade with 6 cm of lime hemp plaster. The sensitivity analysis reveals that
708 the proposed method is robust with respect to the different decision maker's preferences. However,
709 there are several limitations to the proposed methodology. The method requires working on a set
710 of effective thermal renovation solutions determined by the group decision in the alternative
711 generation step. In subsequent work, the use of multi-objective optimization method in this step
712 can be studied. It will help decision makers to reduce the research area, only the relevant solutions
713 regarding the specificity of the existing building would be taken into account. Furthermore,
714 different uncertainties that can affect the final ranking were not taken into account by the method.
715 For future research, it would be relevant to consider uncertainties concerning the evaluation of the
716 criteria and uncertainties regarding the decision-makers preferences.

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